

# Controlling inflation with timid monetary-fiscal regime changes

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  - How expectations of future policy switch affects: (i) equilibria; (ii) dynamics
- Characterize the properties of the economy when both monetary and fiscal policies change over time

# Motivation: Monetary and Fiscal Policy Interaction

Leeper (1991): Equilibria under *active* and *passive* monetary and fiscal policies

	AM	PM
AF	Explosiveness	Determinacy (non-Ricardian case, FTPL)
PF	Determinacy (Ricardian case)	Indeterminacy

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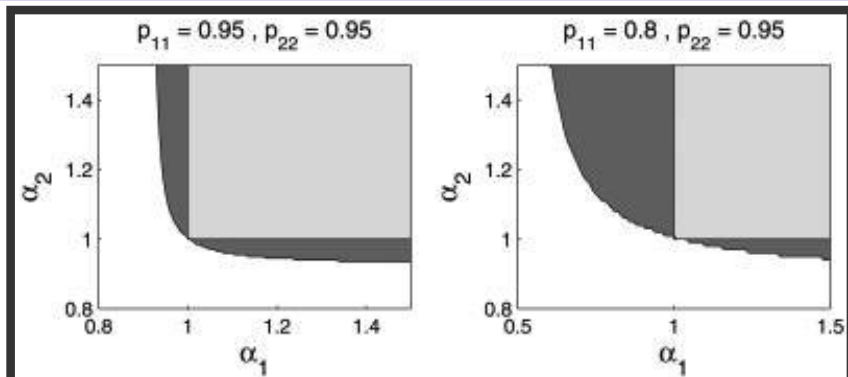
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However, policy regimes change over time → **Expectations about future policies** are crucial: affects dynamics and eq. uniqueness

# The Long-run Taylor principle

Davig and Leeper (2007, AER): Markov switching in monetary policy rule



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→ allows **timid temporary** deviations

**Dynamics** **Cross-regime spillovers:** equilibrium properties are “contaminated” both by the characteristics of the other regimes and by the probability of shifting towards those alternative regimes

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- 1 **Equilibrium properties: uniqueness** → specify the role of fiscal policy (extending Davig-Leeper, 2007)
- 2 **Dynamics: wealth effects vs Ricardian** → expectation effects/cross-regime spillovers in IRFs
- 3 **Policy implications:** → Useful framework to interpret the data: Great Moderation, policy response to the Great Recession

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- Conditions that a switching fiscal policy needs to satisfy to yield a unique rational expectations, when MP is always active
- Similar to LRTP: the long-run fiscal principle entails some fiscal policy flexibility: it could deviate from PF substantially for brief periods or timidly for prolonged periods.

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- overall AM/PF mix ⇒ NO WEALTH EFFECTS
- overall switching mix ⇒ WEALTH EFFECTS

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## ⑤ Application to ZLB and US data

- BVAR on US data for the recent ZLB period  $\Rightarrow$  IRFs: a deficit shock do not spur inflation
- ZLB + “timidity” in fiscal action  $\Rightarrow$  multiple equilibria  $\Rightarrow$  agents coordinating on the solution with no wealth effects



# Related literature

## Regime changes in monetary policy

- Davig and Leeper (2007)  $\Rightarrow$  determinacy condition (LRTP)
- Liu, Waggoner and Zha (2009)  $\Rightarrow$  asymmetric expectation effects under the dovish and the hawkish monetary regime
- Bianchi (2013)  $\Rightarrow$  counterfactuals to show how equilibrium outcomes depend on agents' beliefs about alternative dovish or hawkish monetary regimes

## Related literature

### Regime changes in both monetary and fiscal policies

- Davig and Leeper (2006, 2011), Chung, Davig and Leeper (2007), Bianchi (2012), Bianchi and Ilut (2014)  $\Rightarrow$  Estimate Markov switching monetary and fiscal regimes for the U.S. and study the impact of policy shocks employing actual and counterfactual IRF
- Bhattarai, Lee and Park (2012): allow for indeterminacy in the estimate à la Lubik and Schorfheide (2004)  $\Rightarrow$  PM/PF in pre-Volcker, AM/PF in post-Volcker
- Bianchi and Melosi (2013, 2016)  $\Rightarrow$  study the link between inflation and fiscal imbalances

## Related literature

Technical literature on solving DSGE models with MS parameters

- Blake-Zampolli (2006), Davig-Leeper (2007), Farmer-Waggoner-Zha (2009, 2011), Cho (2014), Foerster (2013), **Foester-Rubio Ramirez-Waggoner-Zha (2014)**, Maih (2014), Barthelemy-Marx (2015)

# Model: simple structure in nonlinear form

$$1 = \beta \mathbb{E}_t \left( \frac{Y_t - G}{Y_{t+1} - G} \frac{R_t}{\Pi_{t+1}} \right), \quad (\text{Euler eq.})$$

$$\begin{aligned} \phi_t \left( 1 - \alpha \Pi_t^{\theta-1} \right)^{\frac{1}{1-\theta}} &= \frac{\mu \theta (1 - \alpha)^{\frac{1}{1-\theta}}}{\theta - 1} Y_t \\ &+ \alpha \beta \mathbb{E}_t \left[ \phi_{t+1} \Pi_{t+1}^{\theta} \left( 1 - \alpha \Pi_{t+1}^{\theta-1} \right)^{\frac{1}{1-\theta}} \right], \end{aligned} \quad (\text{NKPC})$$

$$\phi_t = \frac{Y_t}{Y_t - G} + \alpha \beta \mathbb{E}_t \left( \Pi_{t+1}^{\theta-1} \phi_{t+1} \right),$$

$$\frac{b_t}{R_t} = \frac{b_{t-1}}{\Pi_t} + G - \tau_t, \quad \text{with } b_t = \frac{B_t}{P_t}. \quad (\text{govt b.c.})$$

# Fiscal and Monetary Policy Rules

## Fiscal policy

$$\tau_t = \tau_{ss} \left( \frac{b_{t-1}}{b_{ss}} \right)^{\gamma_\tau(s_t)} e^{\sigma_\tau u_{\tau,t}}$$

## Monetary policy

$$R_t = R_{ss} (\Pi_t)^{\gamma_\pi(s_t)} e^{\sigma_r u_{m,t}}$$

both depend on the underlying Markov process  $s_t$

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- Stability: Mean Square Stable
- Unique solution when a single MSV MSS solution exists

◀ Appendix Method

# Uniqueness under fixed coefficients

Recasting Leeper (1991) in the context of our model

monetary policy **active (AM)** when

$$\gamma_{\pi} > 1$$

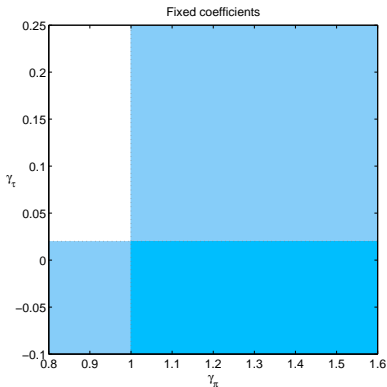
and **passive (PM)** otherwise

fiscal policy **passive (PF)** when  $\left| \frac{1}{\beta} - \frac{1}{\beta} \frac{\tau_{ss}}{b_{ss}} \gamma_{\tau} \right| < 1$ , i.e.

$$\gamma_{\tau} > \frac{b_{ss}}{\tau_{ss}} (1 - \beta) = 0.0196$$

and **active (AF)** otherwise (e.g.  $\gamma_{\tau} = 0$ )

# Uniqueness under fixed coefficients



AM/PF uniqueness

PM/AF uniqueness

PM/PF multiplicity

AM/AF no stable solutions

# Uniqueness under regime switching

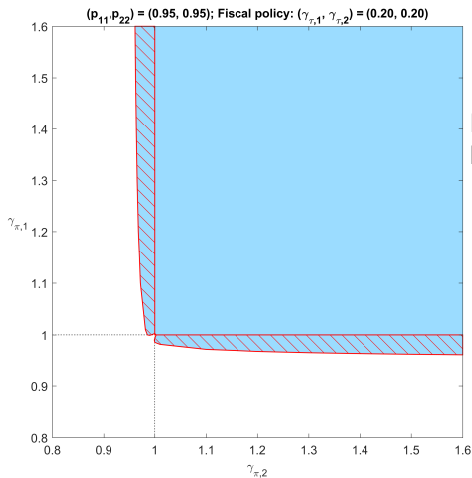
- We consider two regimes:  $s_t = 1, 2$
- Contemporaneous switching in monetary and fiscal policy
- We focus on scenarios where one regime is AM/PF
- Reduce to a two dimensional graph:
  - fix a given (monetary or fiscal) policy in both regimes
  - fix a given regime (AM/PF)

# The Monetary Policy Frontier (MPF)

Given Passive Fiscal Policy (Davig and Leeper, 2007)

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Given Passive Fiscal Policy (Davig and Leeper, 2007)



If fiscal policy stays passive in both regimes

- back to Davig and Leeper's **Long-Run Taylor Principle**
- uniqueness allows timid deviations into PM → **overall AM**

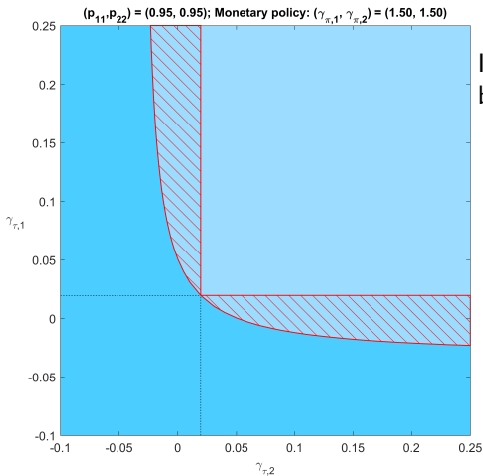
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Given Active Monetary Policy



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Given Active Monetary Policy



If monetary policy stays active in both regimes

- Long-Run Fiscal Principle  
→ uniqueness above the fiscal policy frontier
- uniqueness allows timid deviations into AF → overall PF
- MPF unaffected if LRFP holds (above FPF)

# The Fiscal Policy Frontier (FPF)

## Proposition. The FPF and the long-run Fiscal Principle

For any policy parameter combination, there always exists a particular solution such that in each regime:

$$h_i = \frac{1}{\beta} (1 - \frac{\tau}{b} \gamma_{\tau,i}) \equiv \bar{h}_i(\gamma_{\tau,i}) \text{ and } g_{\pi,i} = 0, \text{ for } i = 1, 2.$$

Then, this solution:

- (i) Is MSS, if above the Fiscal Policy Frontier (eq. (22));
- (ii) Depends only on  $\gamma_{\tau,i}$  for  $i = 1, 2$ , and it is independent of the monetary policy coefficients;
- (iii) If MSS, it yields no wealth effects in both regimes because  $g_{\pi,i} = 0$ , so it is a **Ricardian solution**.

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  - for example ( $\gamma_{\pi,1} = 1.5$ )

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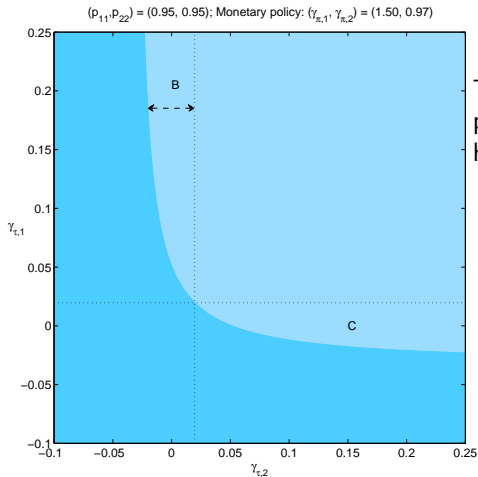
# Switching Policies

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- consider an AM regime 1
  - for example ( $\gamma_{\pi,1} = 1.5$ )
- the central bank switches to PM in regime 2...
- How should fiscal policy be in order to have uniqueness?
  - Need to distinguish two cases: **timid vs. substantial** switch

# Timid Switching Monetary Policy

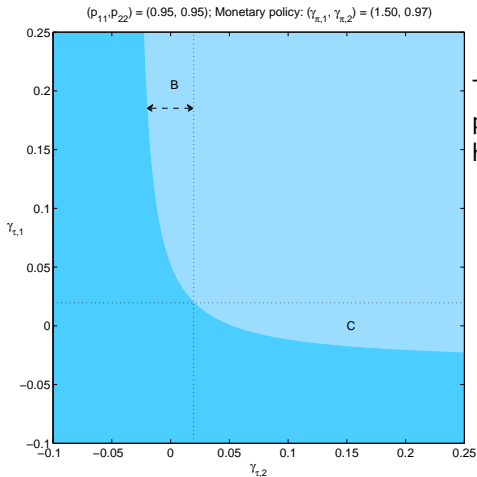
Timid monetary deviation: ( $\gamma_{\pi,2} = 0.97$ )



Timid deviations in monetary policy within the MPF: LRTP holds  $\Rightarrow$  Overall AM

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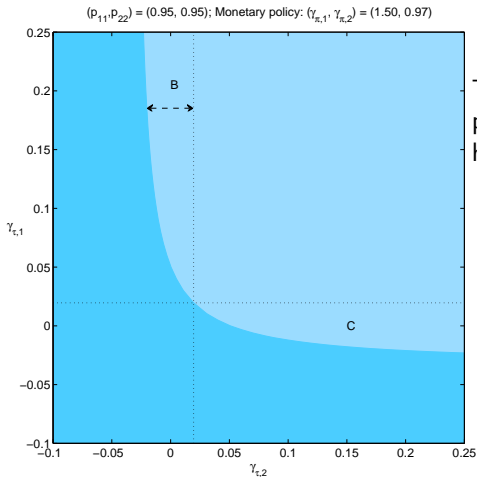


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$\rightarrow$  uniqueness preserved above FPF  $\Rightarrow$  timid deviations into AF  $\Rightarrow$  overall PF

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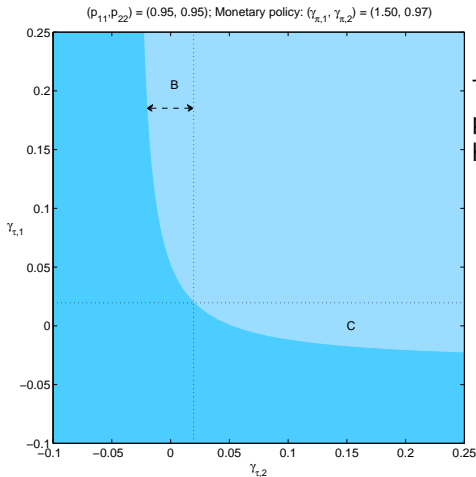
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- $\rightarrow$  **Overall AM/PF Mix**



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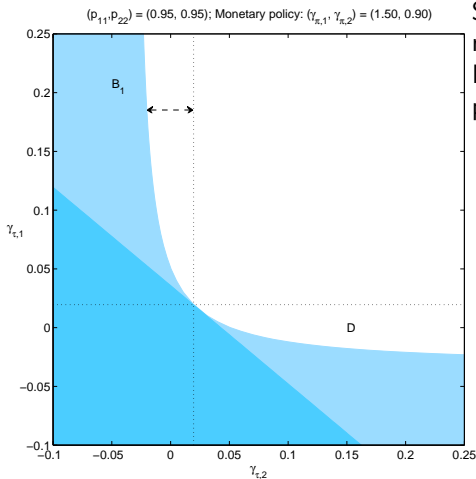


Timid deviations in monetary policy within the MPF: LRTP holds  $\Rightarrow$  Overall AM

- $\rightarrow$  uniqueness preserved above FPF  $\Rightarrow$  timid deviations into AF  $\Rightarrow$  overall PF
- $\rightarrow$  **Overall AM/PF Mix**
- $\rightarrow$  one Ricardian solution  $\Rightarrow$  no wealth effects

# Switching Monetary Policy

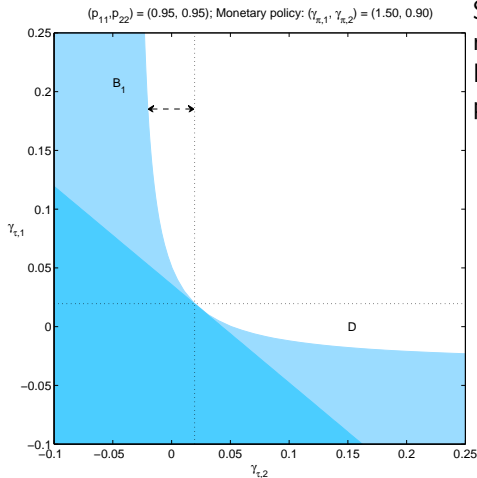
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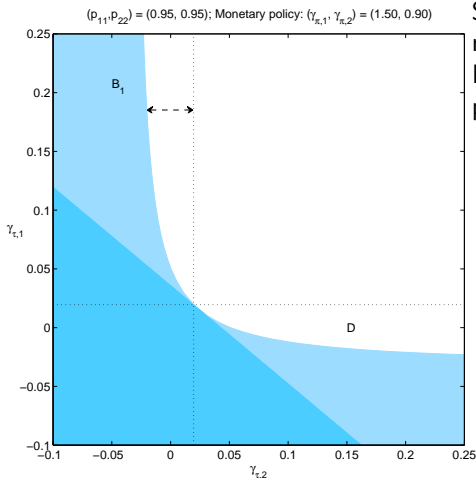


Substantial deviations in monetary policy outside the MPF  $\Rightarrow$  Switching monetary policy

$\rightarrow$  Uniqueness if substantial deviation in fiscal policy:  
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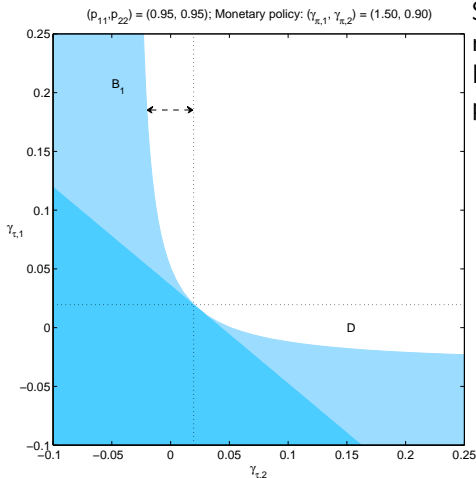


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Substantial deviations in monetary policy outside the MPF  $\Rightarrow$  Switching monetary policy

- $\rightarrow$  Uniqueness if substantial deviation in fiscal policy: Switching fiscal policy
- $\rightarrow$  multiplicity instead if overall passive FP (MPF - LRTP unsatisfied)
- $\rightarrow$  **Overall Switching Policies Mix**: above the straight line: one fiscal unbacking solution  $\Rightarrow$  wealth effects

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**Overall PF:** fiscal policy combination inside Fiscal Policy Frontier  $\Rightarrow$  only timid deviations into AF are allowed



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**Overall AM/PF Mix:** overall AM + overall PF  
 $\Rightarrow$  **Ricardian solution:** no wealth effects in both regimes

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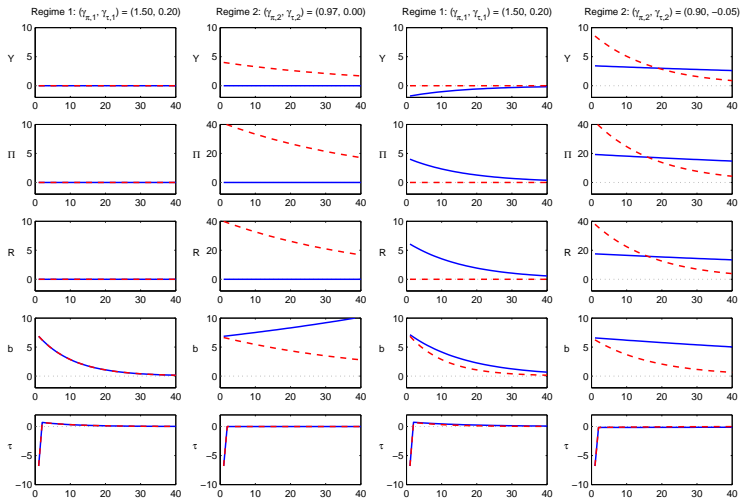
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**Overall switching fiscal policy:** fiscal policy combinations outside Fiscal Policy Frontier  $\Rightarrow$  substantial deviations into AF

**Overall SWITCHING Mix:** overall switching monetary policy + overall switching fiscal policy  $\Rightarrow$  **Non-Ricardian solution:** wealth effects in both regimes

# IRFs to a tax shock under MS and fixed coefficients

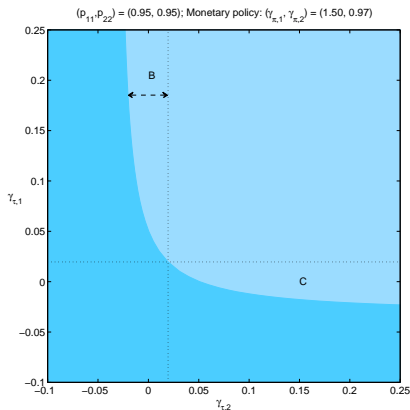


Overall AM/PF Mix

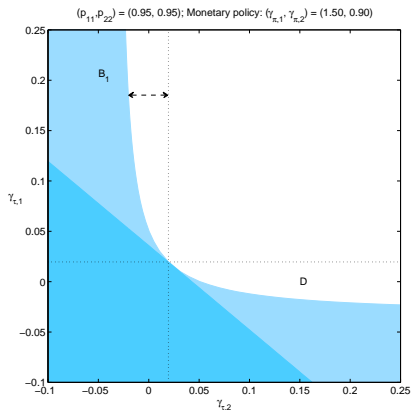
Overall Switching Mix

Blue solid lines: MS; Red dashed lines: fixed coefficients

# The importance of coordination



Modest deviations



Substantial deviations

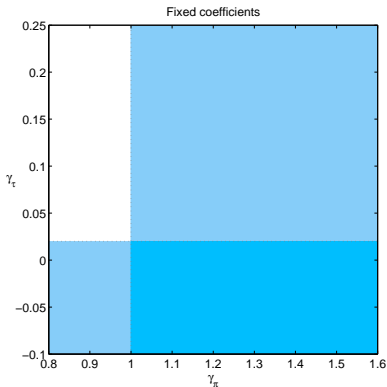
▶ original taxonomy of little use

# What determines uniqueness?

**How to define timid vs. substantial deviations?**



# Uniqueness under fixed coefficients



AM/PF uniqueness

PM/AF uniqueness

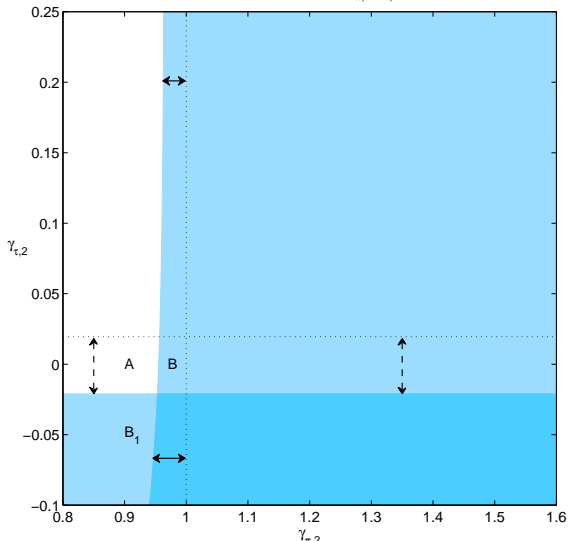
PM/PF multiplicity

AM/AF no stable solutions

# Uniqueness under regime switching

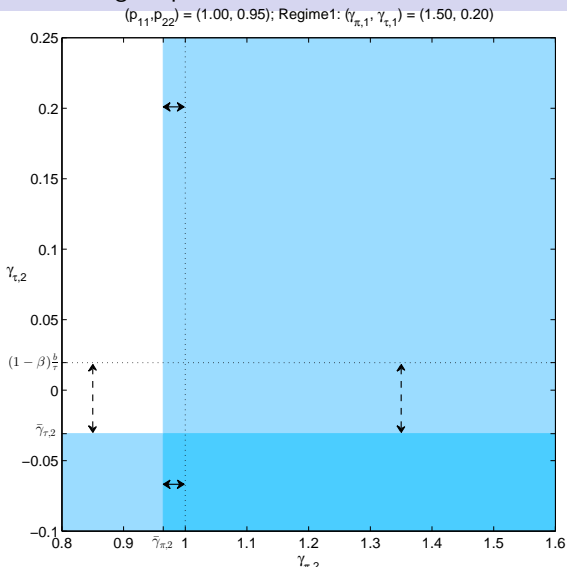
“Timid” deviations: relaxing Leeper’s conditions

$(p_{11}, p_{22}) = (0.95, 0.95)$ ; Regime1:  $(\gamma_{\pi,1}, \gamma_{\tau,1}) = (1.50, 0.20)$



# Uniqueness under regime switching: absorbing case

“Timid” deviations: relaxing Leeper’s conditions



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“Timid” deviations: relaxing Leeper’s conditions

If regime 1 is AM/PF and absorbing, uniqueness:

Upper-right region

$$\gamma_{2,\tau} > \frac{b_{ss}}{\tau_{ss}} \left( 1 - \frac{\beta}{\sqrt{p_{22}}} \right)$$

$$\gamma_{2,\pi} > \sqrt{p_{22}} - \frac{(1 - \beta\sqrt{p_{22}})(1 - \sqrt{p_{22}})}{\lambda}$$

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$$\text{PF: } \gamma_{\tau} > \frac{b_{ss}}{\tau_{ss}} (1 - \beta)$$

$$\gamma_{2,\pi} > \sqrt{p_{22}} - \frac{(1 - \beta \sqrt{p_{22}})(1 - \sqrt{p_{22}})}{\lambda}$$

$$\text{AM: } \gamma_{\pi} > 1$$

# Uniqueness under regime switching: absorbing case

“Timid” deviations: relaxing Leeper’s conditions

If regime 1 is AM/PF and absorbing, uniqueness:

Upper-right region

$$\gamma_{2,\tau} > \frac{b_{ss}}{\tau_{ss}} \left( 1 - \frac{\beta}{\sqrt{p_{22}}} \right) \quad \text{PF: } \gamma_{\tau} > \frac{b_{ss}}{\tau_{ss}} (1 - \beta)$$

$$\gamma_{2,\pi} > \sqrt{p_{22}} - \frac{(1 - \beta \sqrt{p_{22}})(1 - \sqrt{p_{22}})}{\lambda} \quad \text{AM: } \gamma_{\pi} > 1$$

→ **timid deviations from AM and PF still grant uniqueness**

→ Same intuition as for Davig & Leeper for the LRTP

# Uniqueness under regime switching: absorbing case

“Timid” deviations: relaxing Leeper’s conditions

If regime 1 is AM/PF and absorbing, uniqueness:

Upper-right region

$$\gamma_{2,\tau} > \frac{b_{ss}}{\tau_{ss}} \left( 1 - \frac{\beta}{\sqrt{p_{22}}} \right) \quad \text{PF: } \gamma_{\tau} > \frac{b_{ss}}{\tau_{ss}} (1 - \beta)$$

$$\gamma_{2,\pi} > \sqrt{p_{22}} - \frac{(1 - \beta \sqrt{p_{22}})(1 - \sqrt{p_{22}})}{\lambda} \quad \text{AM: } \gamma_{\pi} > 1$$

- timid deviations from AM and PF still grant uniqueness
- Same intuition as for Davig & Leeper for the LRTP
- **deviations can be larger the smaller  $p_{22}$**

# Uniqueness under regime switching: absorbing case

“Timid” deviations: relaxing Leeper’s conditions

## Lower-left region

$$\gamma_{2,\tau} < \frac{b_{ss}}{\tau_{ss}} \left( 1 - \frac{\beta}{\sqrt{p_{22}}} \right)$$

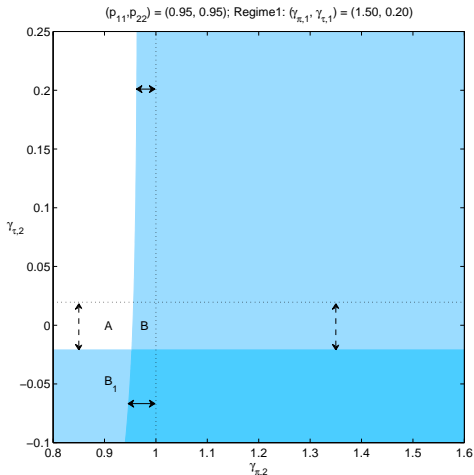
$$\gamma_{2,\pi} < \sqrt{p_{22}} - \frac{(1 - \beta\sqrt{p_{22}})(1 - \sqrt{p_{22}})}{\lambda}$$

- monetary policy needs to deviate substantially from AM
- fiscal policy needs to deviate substantially from PF
- **substantial** and **coordinated** deviations to get uniqueness



# Dynamic response of the model

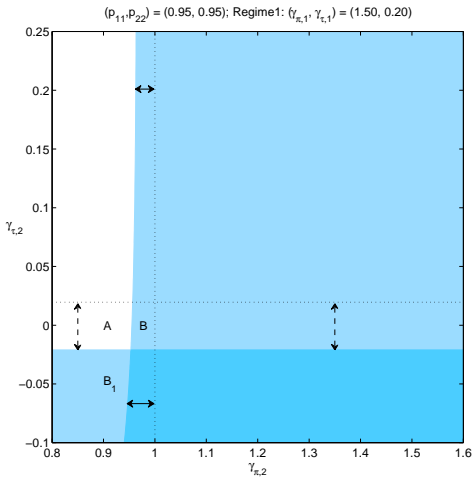
Does the two solutions  $B$  and  $B_1$  exhibit different dynamics?



**Main Intuition:  
A New Taxonomy**

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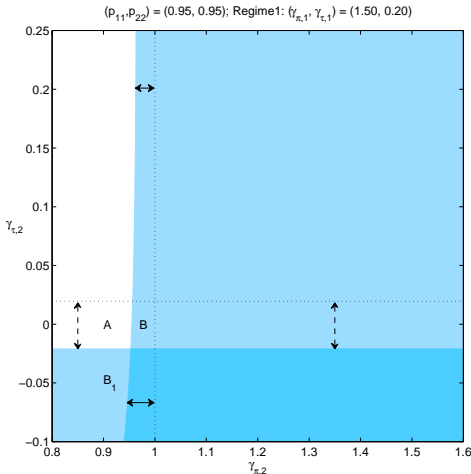


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$B \rightarrow$  Timid deviations from AM and PF

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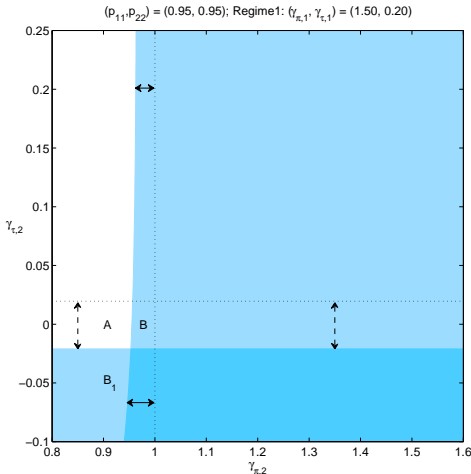


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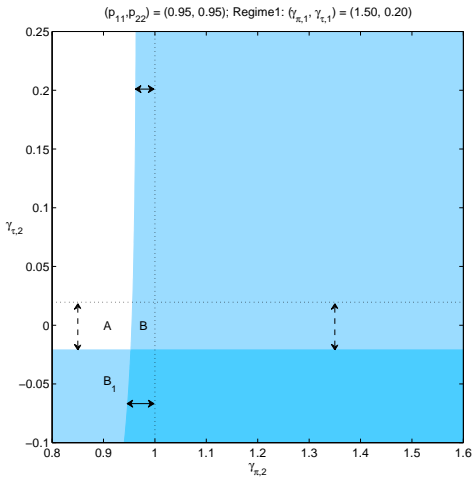


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- $\rightarrow$  **No wealth effects**

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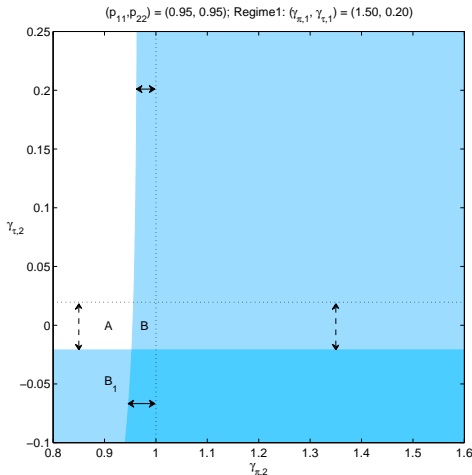


## Main Intuition: A New Taxonomy

- $B$  → Timid deviations from AM and PF
- Overall AM/PF Mix
- No wealth effects
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# Dynamic response of the model

Does the two solutions  $B$  and  $B_1$  exhibit different dynamics?



**Main Intuition:  
A New Taxonomy**

$B$  → Timid deviations from  
AM and PF

→ **Overall AM/PF Mix**

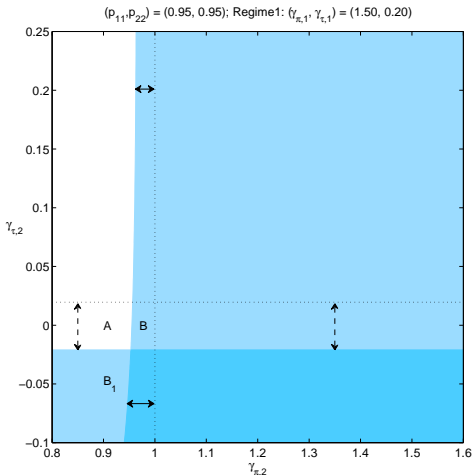
→ **No wealth effects**

$B_1$  → Substantial deviations  
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→ **Overall Switching Mix**

# Dynamic response of the model

Does the two solutions  $B$  and  $B_1$  exhibit different dynamics?



**Main Intuition:  
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$B$  → Timid deviations from AM and PF

→ **Overall AM/PF Mix**

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→ **Overall Switching Mix**

→ **Wealth effects**

# Policy Implications

## Several Implications

- 1 Establish conditions for dynamics to exhibit wealth effects with MS changes



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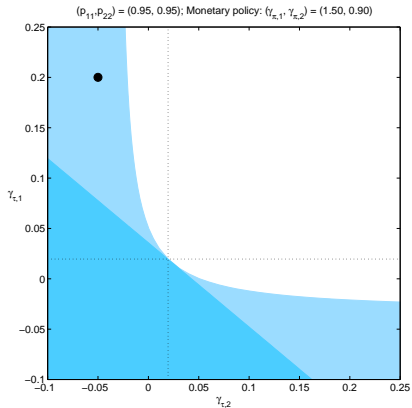
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  - estimation and multiple equilibria

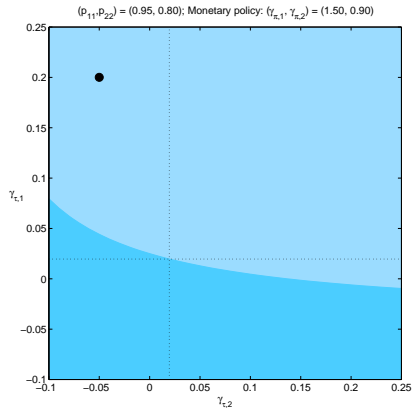
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  - *overall* policy stance matters
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- 5 Regime persistence is key (Bianchi and Melosi, 2013) → define “timid deviations”, MPF and FPF, and type of regimes



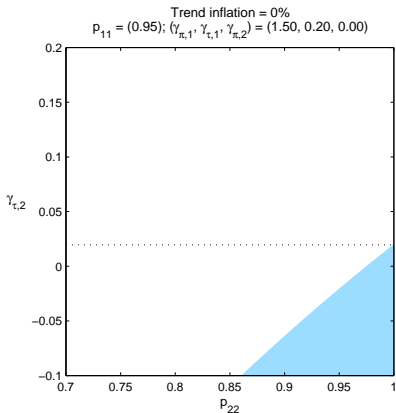
$p_{22} = 0.95$



$p_{22} = 0.80$

# ZLB: Matching theory and evidence

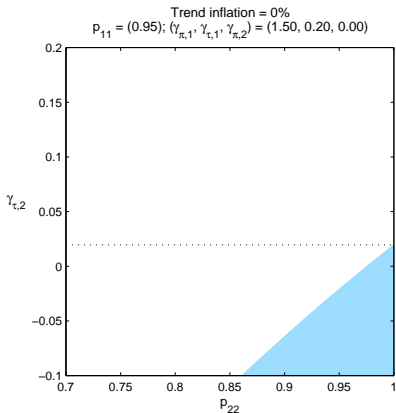
Assume expected AM/PF and  
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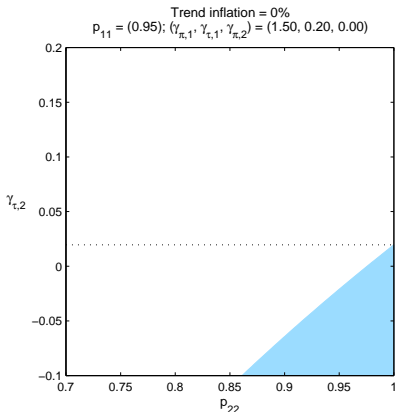
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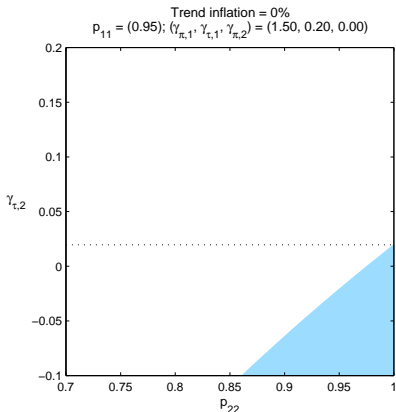


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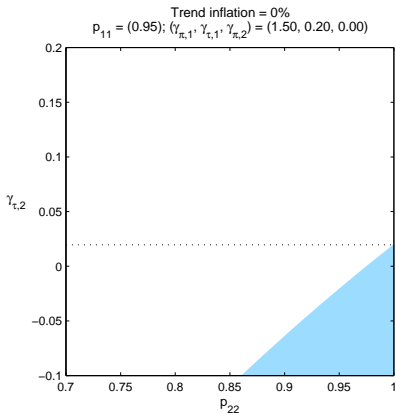
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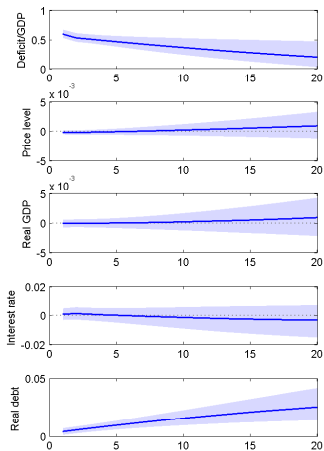
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- Switching regime  $\Rightarrow$  wealth effects

# ZLB: Matching theory and evidence

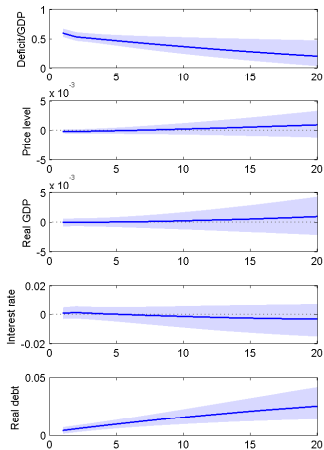
IRFs to a deficit shock from a BVAR on US data 2008q4 - 2015q4

- Output and inflation do not move, debt increases



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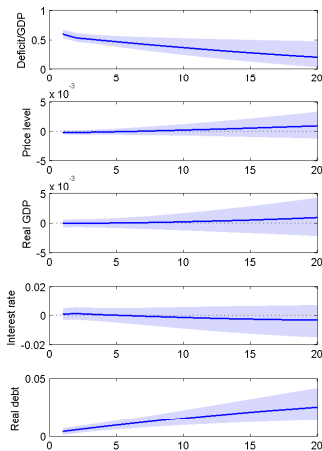
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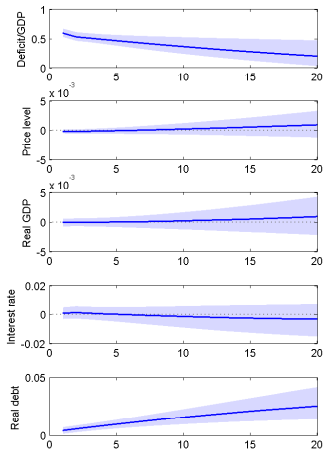
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- Output and inflation do not move, debt increases
- Consistent with PM/AF regime in an overall AM/PF mix  $\Rightarrow$  timid AF and indeterminate equilibrium
- Agents coordinating on the Ricardian one
- More aggressive active fiscal policy  $\Rightarrow$  unique switching mix  $\Rightarrow$  inflation upswing

# Conclusions

In this paper we study the equilibria in a model with shifts in monetary and fiscal policy.

Research questions:

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Is fiscal policy getting in the way?



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Research questions:

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Is fiscal policy getting in the way?
  - **Long-run Fiscal Principle:** timid deviation from PF to avoid wealth effects and enhance CB's controllability of inflation
- Need/gain from coordination?
  - **New Taxonomy** for uniqueness in MS:
    - Overall AM/PF mix  $\Rightarrow$  No wealth effects
    - Overall Switching mix  $\Rightarrow$  wealth effects from FTPL

# Methodology

Following FRWZ, our model can be written as

$$\mathbb{E}_t \mathbf{f}(\mathbf{y}_{t+1}, \mathbf{y}_t, \mathbf{x}_t, \mathbf{x}_{t-1}, \varepsilon_{t+1}, \varepsilon_t, \boldsymbol{\theta}(s_{t+1}), \boldsymbol{\theta}(s_t)) = \mathbf{0}$$

$$\mathbf{x}_t = b_t, \quad \mathbf{y}'_t = [Y_t, \Pi_t, \phi_t, R_t]', \quad \boldsymbol{\theta}'(s_t) = [\gamma_\pi(s_t), \gamma_\tau(s_t)]'.$$

We look for recursive solutions in form

$$\mathbf{x}_t = \mathbf{h}_{s_t}(\mathbf{x}_{t-1}, \varepsilon_t, \chi)$$

$$\mathbf{y}_t = \mathbf{g}_{s_t}(\mathbf{x}_{t-1}, \varepsilon_t, \chi)$$

perturbed around the non-stochastic steady state  $[\bar{\mathbf{x}}, \bar{\mathbf{y}}]$ . Note that the **solutions are regime-dependent**, while the steady state is not.

- Under regime  $i$ , the first order Taylor expansion of the solutions are

$$b_t \approx \bar{b} + h_{i,b}(b_{t-1} - \bar{b}) + h_{i,\varepsilon}\varepsilon_t + h_{i,\chi}\chi$$

$$y_t \approx \bar{y} + g_{i,b}(b_{t-1} - \bar{b}) + g_{i,\varepsilon}\varepsilon_t + g_{i,\chi}\chi$$

with the partial derivatives evaluated at the steady state.

- The derivatives of  $\mathbb{E}_t \mathbf{f}$  are equal to zero and depend on the unknown coefficients  $h_{i,b}$ ,  $h_{i,\varepsilon}$ ,  $h_{i,\chi}$ ,  $g_{i,b}$ ,  $g_{i,\varepsilon}$ ,  $g_{i,\chi}$ .
- FRWZ show that the  $h_{i,b}$  and  $g_{i,b}$  are the roots of a separated system of quadratic equations, unsolvable with standard methods (Gensys, etc.)
- We use Matlab's Symbolic Toolbox to get all the solutions.

# Stability

We use the concept of **mean square stability** (Costa et al. 2005)

→ MSS requires the existence of

$$\lim_{t \rightarrow \infty} \mathbb{E}_0 \left( \begin{bmatrix} \mathbf{x}_t \\ \mathbf{y}_t \end{bmatrix} \right), \quad \text{and} \quad \lim_{t \rightarrow \infty} \mathbb{E}_0 \left( \begin{bmatrix} \mathbf{x}_t \\ \mathbf{y}_t \end{bmatrix} \begin{bmatrix} \mathbf{x}_t \\ \mathbf{y}_t \end{bmatrix}' \right)$$

→ different concept of stability w.r.t. boundedness

→ see Farmer et al. (2009) for a discussion in the context of MS-DSGEs

→ with 2 regimes and 1 state variable, the solution  $(h_{1,b}, h_{2,b})$  is MSS if

$$\begin{bmatrix} p_{11} h_{1,b}^2 & (1 - p_{22}) h_{2,b}^2 \\ (1 - p_{11}) h_{1,b}^2 & p_{22} h_{2,b}^2 \end{bmatrix}$$

has all its eigenvalues inside the unit circle.

[◀ Back to Methodology](#)

# Original taxonomy of little use

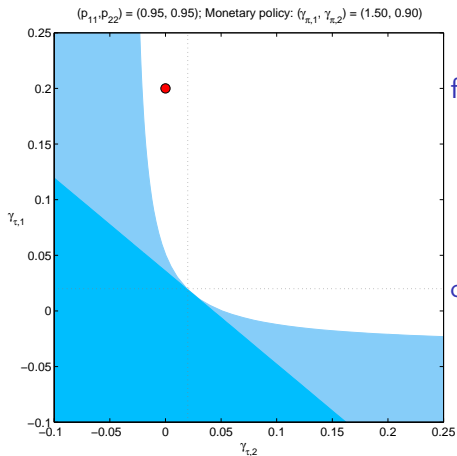
What happens when both monetary and fiscal policy shift?

## **Original taxonomy of little use**

- the clear cut results by Leeper (1991) are lost
- policies must coordinate to get a determinate equilibrium
- the expectation of a stable regime in the future is not sufficient to get uniqueness

# Original taxonomy of little use

Point A first Figure: AM/PF + PM/AF = multiplicity



fixed coefficients taxonomy

reg1 AM/PF:

$$\gamma_{\pi,1} = 1.5, \gamma_{\tau,1} = 0.2$$

reg2 PM/AF:

$$\gamma_{\pi,2} = 0.9, \gamma_{\tau,2} = 0$$

our taxonomy

glob. switching monetary policy

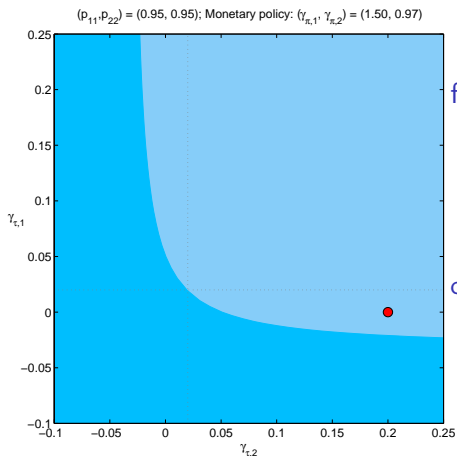
+ glob. passive fiscal policy

→ no coordination, multiplicity



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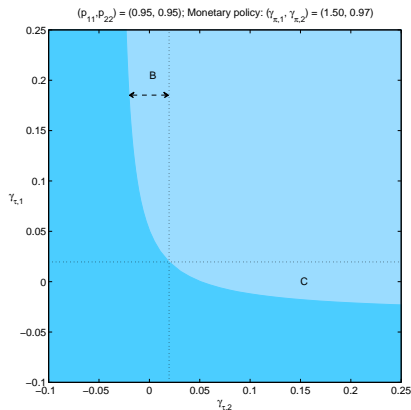
$$\gamma_{\pi,2} = 0.97, \gamma_{\tau,2} = 0.2$$

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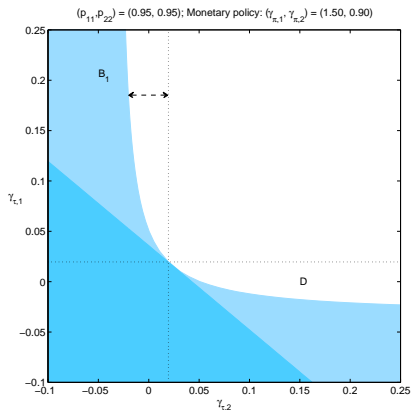
glob. active monetary policy +  
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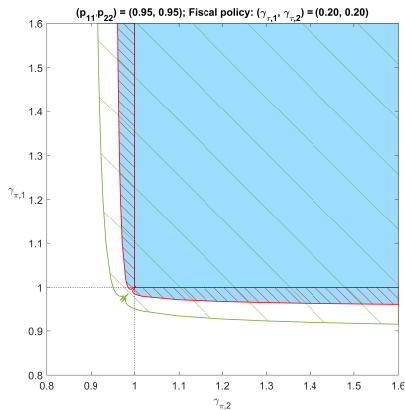
Modest deviations



Substantial deviations

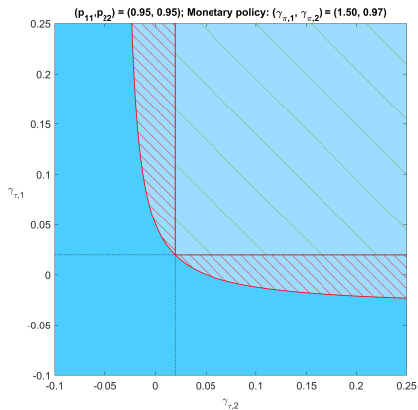
[▶ back to new taxonomy](#)

# MSS vs BRS



Modest deviations

▶ [back to policy implications](#)



Substantial deviations