Financial Constraints and Firms Dynamics

Andrea Caggese (UPF, CREI, and Barcelona GSE)

October 16, 2013

 Firm dynamics: ongoing process of entry, growth, and exit of firms.

- Firm dynamics: ongoing process of entry, growth, and exit of firms.
 - It determines the cross sectional distribution of active firms at any point in time.

- Firm dynamics: ongoing process of entry, growth, and exit of firms.
 - It determines the cross sectional distribution of active firms at any point in time.
 - Large reallocation across productive units: most studies find annual job reallocation between 15% and 30% for industrialized countries.

- Firm dynamics: ongoing process of entry, growth, and exit of firms.
 - It determines the cross sectional distribution of active firms at any point in time.
 - Large reallocation across productive units: most studies find annual job reallocation between 15% and 30% for industrialized countries.
 - Firms in an industry are very heterogeneous in terms of size and productivity.
 - Syverson (2004): on average, in a 4 digit US manufacturing sector, a plant at the 90th percentile of productivity makes twice the output, with the same inputs, than a plant at the 10th percentile.

- Firm dynamics: ongoing process of entry, growth, and exit of firms.
 - It determines the cross sectional distribution of active firms at any point in time.
 - Large reallocation across productive units: most studies find annual job reallocation between 15% and 30% for industrialized countries.
 - Firms in an industry are very heterogeneous in terms of size and productivity.
 - Syverson (2004): on average, in a 4 digit US manufacturing sector, a plant at the 90th percentile of productivity makes twice the output, with the same inputs, than a plant at the 10th percentile.
- The factors that determine firm dynamics are important for aggregate productivity.

- Firm dynamics are affected by:
 - Factors related to the production technology:

- Firm dynamics are affected by:
 - Factors related to the production technology:
 - Learning, Innovation, Technology adoption.
 - Adjustment costs, Search frictions.

- Firm dynamics are affected by:
 - Factors related to the production technology:
 - Learning, Innovation, Technology adoption.
 - Adjustment costs, Search frictions.
 - Competition.
 - Institutional Factors.

- Firm dynamics are affected by:
 - Factors related to the production technology:
 - Learning, Innovation, Technology adoption.
 - Adjustment costs, Search frictions.
 - Competition.
 - Institutional Factors.
 - Bureaucracy, taxes, legal constraints, etc...

- Firm dynamics are affected by:
 - Factors related to the production technology:
 - Learning, Innovation, Technology adoption.
 - Adjustment costs, Search frictions.
 - Competition.
 - Institutional Factors.
 - Bureaucracy, taxes, legal constraints, etc...
 - Financial frictions.

Financial factors: why are they important?

Financial factors: why are they important?

Small and young firms are financially constrained.

Financial factors: why are they important?

- Small and young firms are financially constrained.
- In Firm Dynamics models, financial frictions predict a life cycle behavior of firms consistent with stylized facts (e.g., Clementi and Hopenhayn, 2006).

Financial factors: why are they important?

- Small and young firms are financially constrained.
- In Firm Dynamics models, financial frictions predict a life cycle behavior of firms consistent with stylized facts (e.g., Clementi and Hopenhayn, 2006).

Younger firms:

- Are smaller.
- Grow faster.
- Have an higher variance of growth rates.
- Have an higher probability of exit.

Financial factors: why are they important?

- Small and young firms are financially constrained.
- In Firm Dynamics models, financial frictions predict a life cycle behavior of firms consistent with stylized facts (e.g., Clementi and Hopenhayn, 2006).

Younger firms:

- Are smaller.
- Grow faster.
- Have an higher variance of growth rates.
- Have an higher probability of exit.
- Financial factors explain cross country differences in productivity.

Financial factors: why are they important?

- Small and young firms are financially constrained.
- In Firm Dynamics models, financial frictions predict a life cycle behavior of firms consistent with stylized facts (e.g., Clementi and Hopenhayn, 2006).

Younger firms:

- Are smaller.
- Grow faster.
- Have an higher variance of growth rates.
- Have an higher probability of exit.
- Financial factors explain cross country differences in productivity.
- Oredit cycle models with heterogeneous firms.



Outline for this talk

• I will briefly review some recent papers on financial frictions and firm dynamics.

Outline for this talk

- I will briefly review some recent papers on financial frictions and firm dynamics.
 - Financial frictions worsen the allocation of resources across firms, and lower aggregate productivity.
 - Extensive margin possibly more important than the intensive margin.

Outline for this talk

- I will briefly review some recent papers on financial frictions and firm dynamics.
 - Financial frictions worsen the allocation of resources across firms, and lower aggregate productivity.
 - Extensive margin possibly more important than the intensive margin.
- ② I will talk about a work in progress on financial frictions, innovation and firm dynamics.

- Aggregate productivity depends on:
 - How productive individual production units are.
 - How inputs are allocated across them.

- Aggregate productivity depends on:
 - How productive individual production units are.
 - How inputs are allocated across them.
 - Allocation improves when more productive units absorb more inputs.

- Aggregate productivity depends on:
 - How productive individual production units are.
 - How inputs are allocated across them.
 - Allocation improves when more productive units absorb more inputs.
- Misallocation important for cross country differences in aggregate TFP (e.g. Hsieh and Klenow, 2009)

- Aggregate productivity depends on:
 - How productive individual production units are.
 - How inputs are allocated across them.
 - Allocation improves when more productive units absorb more inputs.
- Misallocation important for cross country differences in aggregate TFP (e.g. Hsieh and Klenow, 2009)

- How do financial factors affect the misallocation of resources across firms?
- Intensive margin: Misallocation of capital among active firms.

- How do financial factors affect the misallocation of resources across firms?
- Intensive margin: Misallocation of capital among active firms.
- Extensive Margin :
 - Misallocation of Entry/Exit of firms:
 - Misallocation of other types of "long horizon" investment decisions.

- Misallocation of Entry/Exit of firms:
 - Too few firms enter, and/or of the wrong type (e.g. Buera, Kaboski and Shin, 2011; Caggese and Cunat, 2013).

- Misallocation of Entry/Exit of firms:
 - Too few firms enter, and/or of the wrong type (e.g. Buera, Kaboski and Shin, 2011; Caggese and Cunat, 2013).
- Other types of long horizon investment decisions:
 - Distorted sector selection (e.g. Buera, Kaboski and Shin, 2011)

- Misallocation of Entry/Exit of firms:
 - Too few firms enter, and/or of the wrong type (e.g. Buera, Kaboski and Shin, 2011; Caggese and Cunat, 2013).
- Other types of long horizon investment decisions:
 - Distorted sector selection (e.g. Buera, Kaboski and Shin, 2011)
 - Reduced technology adoption: (e.g. Midrigan and Xu, 2012)

- Misallocation of Entry/Exit of firms:
 - Too few firms enter, and/or of the wrong type (e.g. Buera, Kaboski and Shin, 2011; Caggese and Cunat, 2013).
- Other types of long horizon investment decisions:
 - Distorted sector selection (e.g. Buera, Kaboski and Shin, 2011)
 - Reduced technology adoption: (e.g. Midrigan and Xu, 2012)
 - Reduced entry into foreign markets (e.g. Manova, 2013)

- Misallocation of Entry/Exit of firms:
 - Too few firms enter, and/or of the wrong type (e.g. Buera, Kaboski and Shin, 2011; Caggese and Cunat, 2013).
- Other types of long horizon investment decisions:
 - Distorted sector selection (e.g. Buera, Kaboski and Shin, 2011)
 - Reduced technology adoption: (e.g. Midrigan and Xu, 2012)
 - Reduced entry into foreign markets (e.g. Manova, 2013)
 - Distorted entry into foreign markets (e.g. Caggese and Cunat, 2013)

- Misallocation of Entry/Exit of firms:
 - Too few firms enter, and/or of the wrong type (e.g. Buera, Kaboski and Shin, 2011; Caggese and Cunat, 2013).
- Other types of long horizon investment decisions:
 - Distorted sector selection (e.g. Buera, Kaboski and Shin, 2011)
 - Reduced technology adoption: (e.g. Midrigan and Xu, 2012)
 - Reduced entry into foreign markets (e.g. Manova, 2013)
 - Distorted entry into foreign markets (e.g. Caggese and Cunat, 2013)
 - Distorted Innovation decision (This paper)

Quantitative results

- Buera, Kaboski and Shin (2011): financial frictions explain 60% of the cross-country relation between financial development and TFP.
 - Intensive margin explains almost all of the effect for services sector, and roughly 50% of effect for manufacturing sector.
 - Extensive margin (misallocation of talent) explains other half of effect for manufacturing sector.

Quantitative results

- Buera, Kaboski and Shin (2011): financial frictions explain 60% of the cross-country relation between financial development and TFP.
 - Intensive margin explains almost all of the effect for services sector, and roughly 50% of effect for manufacturing sector.
 - Extensive margin (misallocation of talent) explains other half of effect for manufacturing sector.
- Midrigan and Xu (2012):
 - Sector and Technology selection reduce TFP up to 40%, while misallocation across firms (intensive margin) only accounts for 5% of TFP losses.

Quantitative results

- Buera, Kaboski and Shin (2011): financial frictions explain 60% of the cross-country relation between financial development and TFP.
 - Intensive margin explains almost all of the effect for services sector, and roughly 50% of effect for manufacturing sector.
 - Extensive margin (misallocation of talent) explains other half of effect for manufacturing sector.
- Midrigan and Xu (2012):
 - Sector and Technology selection reduce TFP up to 40%, while misallocation across firms (intensive margin) only accounts for 5% of TFP losses.

- Caggese and Cunat (2013): Financing frictions reduce gains from trade liberalization by 25% (even when they do not reduce the percentage of exporting firms).
 - 70% of this reduction is the indirect effect of distorted entry.

- Caggese and Cunat (2013): Financing frictions reduce gains from trade liberalization by 25% (even when they do not reduce the percentage of exporting firms).
 - 70% of this reduction is the indirect effect of distorted entry.
- Gilchrist, Sim, and Zakrajšek (2012) estimate misallocation (intensive margin) using the dispersion of borrowing costs across US firms. They find small productivity losses, around 3.5% of TFP.

- Caggese and Cunat (2013): Financing frictions reduce gains from trade liberalization by 25% (even when they do not reduce the percentage of exporting firms).
 - 70% of this reduction is the indirect effect of distorted entry.
- Gilchrist, Sim, and Zakrajšek (2012) estimate misallocation (intensive margin) using the dispersion of borrowing costs across US firms. They find small productivity losses, around 3.5% of TFP.

Financing frictions and firm dynamics during recessions.

 Oberfield (2013): Chilean 1982 Financial crisis, Manufacturing output fell by 20%, TFP by 10%.

- Oberfield (2013): Chilean 1982 Financial crisis,
 Manufacturing output fell by 20%, TFP by 10%.
 - Within industry reallocation constant or improved.

- Oberfield (2013): Chilean 1982 Financial crisis,
 Manufacturing output fell by 20%, TFP by 10%.
 - Within industry reallocation constant or improved.
 - Worsening of between industry reallocation contributes to 1/3 drop in TFP
 - \bullet Decline in capacity utilization accounts for around $1/2\ \mathrm{drop}$ in TFP.

- Oberfield (2013): Chilean 1982 Financial crisis,
 Manufacturing output fell by 20%, TFP by 10%.
 - Within industry reallocation constant or improved.
 - Worsening of between industry reallocation contributes to 1/3 drop in TFP
 - Decline in capacity utilization accounts for around 1/2 drop in TFP.
- Khan and Thomas (2013): Calibrated DSGE model with firm dynamics, financing frictions and partial irreversibility.
 - Misallocation resulting from a credit shock generates dynamics consistent with the recent Great Recession.

Summary

• Financial frictions important for firm dynamics

Summary

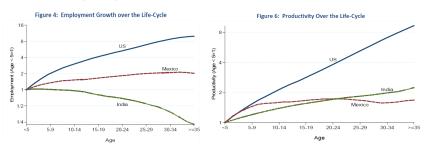
- Financial frictions important for firm dynamics
- Interact with technological factors.
 - Interaction with extensive margins important for industry equilibrium and aggregate TFP.

Summary

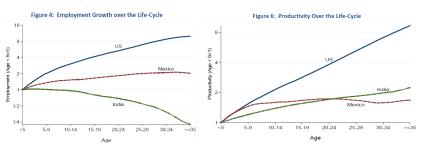
- Financial frictions important for firm dynamics
- Interact with technological factors.
 - Interaction with extensive margins important for industry equilibrium and aggregate TFP.
 - Interaction with adjustment costs along the intensive margin important for cyclical fluctuations.

• Financing frictions, innovation, and productivity growth

- Financing frictions, innovation, and productivity growth
- Within-firm accumulation of intangible capital: Hsieh and Klenow (2012) compare US, India and Mexico:

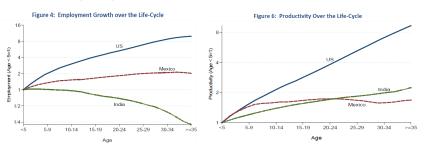


- Financing frictions, innovation, and productivity growth
- Within-firm accumulation of intangible capital: Hsieh and Klenow (2012) compare US, India and Mexico:



• They estimate that moving from the US life cycle of firms to those of India or Mexico could lower aggregate TFP by 25%.

- Financing frictions, innovation, and productivity growth
- Within-firm accumulation of intangible capital: Hsieh and Klenow (2012) compare US, India and Mexico:



- They estimate that moving from the US life cycle of firms to those of India or Mexico could lower aggregate TFP by 25%.
- Financing factors matter? Complementary or alternative to technology based explanations?

This paper

• Do financial factors matter for innovation and productivity growth over the firm life cycle?

This paper

- Do financial factors matter for innovation and productivity growth over the firm life cycle?
- Empirical evidence from firm level Italian data (with balance sheet data, and survey data on innovation and financing frictions).

This paper

- Do financial factors matter for innovation and productivity growth over the firm life cycle?
- Empirical evidence from firm level Italian data (with balance sheet data, and survey data on innovation and financing frictions).
- Industry model with heterogenous firms, entry and exit, costly bankruptcy and risky innovation.

- In the data:
 - In more financially constrained sectors, productivity grows slower over the firm life cycle than in less financially constrained sectors.

In the data:

- In more financially constrained sectors, productivity grows slower over the firm life cycle than in less financially constrained sectors.
- In less financially constrained sectors, firms innovate more on average, and product innovation grows more over the life cycle than in more financially constrained sectors.

In the data:

- In more financially constrained sectors, productivity grows slower over the firm life cycle than in less financially constrained sectors.
- In less financially constrained sectors, firms innovate more on average, and product innovation grows more over the life cycle than in more financially constrained sectors.
- On average product innovation is related to increases in productivity in both constrained and unconstrained sectors.

In the data:

- In more financially constrained sectors, productivity grows slower over the firm life cycle than in less financially constrained sectors.
- In less financially constrained sectors, firms innovate more on average, and product innovation grows more over the life cycle than in more financially constrained sectors.
- On average product innovation is related to increases in productivity in both constrained and unconstrained sectors.

Product innovation is risky:

- Doraszelski and Jaumandreu (2013): innovative activity increases volatility of productivity;
- Caggese (2012): innovation to introduce new products increases volatility of profits more than other types of innovation.

 Monopolistic competition model with heterogenous firms, entry and exit, costly bankruptcy, exogenous technological growth (moving frontier) and innovation:

- Monopolistic competition model with heterogenous firms, entry and exit, costly bankruptcy, exogenous technological growth (moving frontier) and innovation:
 - Firms pay a fixed cost to enter, and learn their productivity.

- Monopolistic competition model with heterogenous firms, entry and exit, costly bankruptcy, exogenous technological growth (moving frontier) and innovation:
 - Firms pay a fixed cost to enter, and learn their productivity.
 - They start with low wealth and cannot borrow. Some young firms may go bankrupt. If they survive, they gradually overcome financing frictions.

- Monopolistic competition model with heterogenous firms, entry and exit, costly bankruptcy, exogenous technological growth (moving frontier) and innovation:
 - Firms pay a fixed cost to enter, and learn their productivity.
 - They start with low wealth and cannot borrow. Some young firms may go bankrupt. If they survive, they gradually overcome financing frictions.
 - New firms enter with a better technology. Existing firms need to innovate, otherwise their profits drop and they eventually exit because of obsolescence.

- Different types of innovation:
 - Type-one, "incremental": if it fails, firm maintains status quo. If it succeeds, its technology improves and keeps up with the exogenous frontier.

- Different types of innovation:
 - Type-one, "incremental": if it fails, firm maintains status quo.
 If it succeeds, its technology improves and keeps up with the exogenous frontier.
 - Type-two, "radical": If it fails, profits drop relative to pre-innovation level, but if it succeeds, the firm reaches the frontier.

- Different types of innovation:
 - Type-one, "incremental": if it fails, firm maintains status quo.
 If it succeeds, its technology improves and keeps up with the exogenous frontier.
 - Type-two, "radical": If it fails, profits drop relative to pre-innovation level, but if it succeeds, the firm reaches the frontier.
 - In equilibrium, the most productive firms engage in type one innovation. Laggard firms either do not innovate or try type two innovation.

- Financing frictions and innovation, the effect is generally ambiguous:
 - Direct effect: Lack of finance reduces innovation for younger firms.

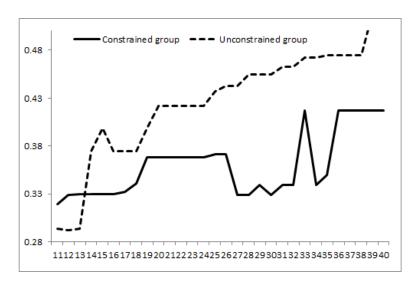
- Financing frictions and innovation, the effect is generally ambiguous:
 - Direct effect: Lack of finance reduces innovation for younger firms.
 - Indirect effect: Reduction in competition increases expected profits of older firms.

- Financing frictions and innovation, the effect is generally ambiguous:
 - Direct effect: Lack of finance reduces innovation for younger firms.
 - Indirect effect: Reduction in competition increases expected profits of older firms.
- For incremental innovation, the indirect effect is positive, and much larger than the negative direct effect. This type of innovation generates counterfactual dynamics.

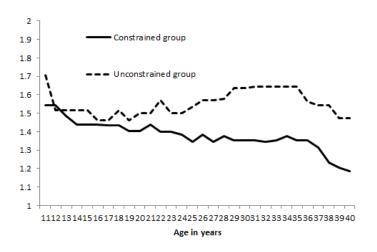
- Financing frictions and innovation, the effect is generally ambiguous:
 - Direct effect: Lack of finance reduces innovation for younger firms.
 - Indirect effect: Reduction in competition increases expected profits of older firms.
- For incremental innovation, the indirect effect is positive, and much larger than the negative direct effect. This type of innovation generates counterfactual dynamics.
- However, the indirect competition effect reduces radical innovation (because of downside risk).

- Financing frictions and innovation, the effect is generally ambiguous:
 - Direct effect: Lack of finance reduces innovation for younger firms.
 - Indirect effect: Reduction in competition increases expected profits of older firms.
- For incremental innovation, the indirect effect is positive, and much larger than the negative direct effect. This type of innovation generates counterfactual dynamics.
- However, the indirect competition effect reduces radical innovation (because of downside risk).
- Once also this type of innovation is possible, innovation dynamics in the model are consistent with the empirical evidence.

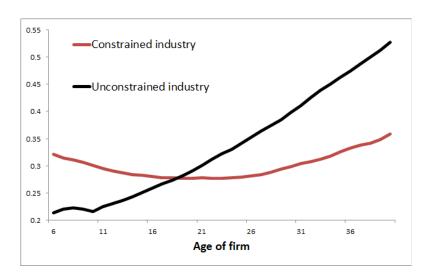
Innovation over the life cycle (empirical data)



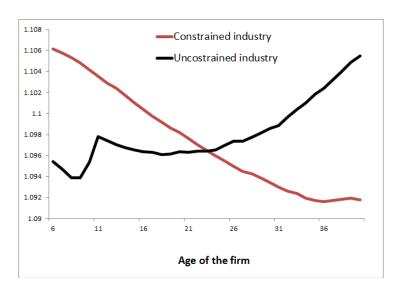
Total factor productivity over the life cycle (data)



Innovation over the life cycle (model simulations)



Productivity over the life cycle (model simulations)



 Empirical analysis shows that financing frictions are correlated to slower innovation growth and productivity growth along the life cycle of firms.

- Empirical analysis shows that financing frictions are correlated to slower innovation growth and productivity growth along the life cycle of firms.
- A calibrated model with heterogenous firms can replicate these dynamics if we introduce the possibility of "radical" innovation.

- Empirical analysis shows that financing frictions are correlated to slower innovation growth and productivity growth along the life cycle of firms.
- A calibrated model with heterogenous firms can replicate these dynamics if we introduce the possibility of "radical" innovation.
- The most important effect of financing frictions on innovation and aggregate productivity is the indirect competition effect.

Empirical data

- I construct a survey based measure of financing constraints.
 - Firms answer questions on difficulty in obtaining loans, or high cost of loans.
- Calculate the percentage of financially constrained firms in each 4 digit manufacturing industry

Empirical data

- I construct a survey based measure of financing constraints.
 - Firms answer questions on difficulty in obtaining loans, or high cost of loans.
- Calculate the percentage of financially constrained firms in each 4 digit manufacturing industry
- Create two groups:
 - The 50% four digit sectors with higher frequency of constrained firms, called the "Constrained" group,
 - The 50% four digit sectors with lower frequency of constrained firms, called the "Unconstrained" group.

Productivity over the life cycle

	. Dependent variable	revenue ba	ased IFP
Most cons	strained sectors	Least con	strained sectors.
-0.115		0.048	
(0.048**)		(0.059)	
	-0.074(0.089)		0.474(0.217**)
	-0.259(0.132**)		0.337(0.319)
	-0.298(0.182)		0.302(0.344)
	-0.374(0.220*)		0.502(0.384)
	-0.472(0.280*)		0.444(0.405)
	-0.480(0.320)		0.497(0.450)
	-0.662(0.361*)		0.693(0.495)
	-0.854(0.407**)		0.607(0.538)
	-0.915(0.449**)		0.682(0.572)
	-1.064(0.456***)		0.888(0.629)
2958	2958	2055	2055
0.020	0.020	0.002	0.002
	-0.115 (0.048**) 2958 0.020	(0.048**) -0.074(0.089) -0.259(0.132**) -0.298(0.182) -0.374(0.220*) -0.472(0.280*) -0.480(0.320) -0.662(0.361*) -0.854(0.407**) -0.915(0.449**) -1.064(0.456***) 2958 2958 0.020 0.020	-0.115

Innovation over the life cycle (2)

Fixed effects regression. Dependent variable: innovation decision						
	R&D section of the survey		Fixed investment section			
	(1) R&D	(2) R&D for	Other R&D	(3) Fixed I.	Other F.I.	
	(1) 1(&D	new products	Other N&D	for new prod.		
Only constrained sectors						
AGE_{it}	0.55 (.46)	0.47 (.51)	-0.34 (.64)	-0.03 (.37)	0.11 (.37)	
n.obs.	329	219	81	407	383	
Pseudo R^2	0.126	0.144	0.091	0.100	0.102	
% of firms inn.	31.4%	15.2%	17.2%	27.0%	62.8%	
Only unconstrained sectors						
AGE_{it}	0.70 (1.0)	2.36 (.9)***	-1.99 (.93)**	1.39 (.58)**	-1.66 (.66)**	
n.obs.	122	135	74	242	221	
Pseudo R^2	0.141	0.100	0.084	0.071	0.070	
% of firms inn.	36.6%	20.3%	17.2%	30.9%	55.5%	

Innovation and productivity

Fixed effects regression. Dependent variable: revenue based TFP					
	All firms	Constr. sectors	Unconst. sectors		
R&D	0.015 (0.029)	0.007 (0.043)	-0.031 (0.066)		
R&D for new products	0.070 (0.027)***	0.114 (0.046)**	0.051 (0.045)		
Other $R\&D$ activity	-0.039 (0.026)	-0.082 (0.039)**	-0.058 (0.048)		
Fixed inv. for new products	0.058 (0.022)***	0.072 (0.034) **	0.075 (0.041)**		
Fixed inv. for current prod.	-0.046 (0.021)**	-0.037 (0.033)	-0.092 (0.048)**		
survey dummies included					

The model

Firm Dynamics monopolistic competition Model a la Hopenhayn (1992) (and Melitz, 2003)

- Each firm in an industry uses labour to produce a variety $w \in \Omega$ of a consumption good.
- Consumers preferences for the varieties in the industry are C.E.S. with elasticity $\sigma>1$.

The model

Firm Dynamics monopolistic competition Model a la Hopenhayn (1992) (and Melitz, 2003)

- Each firm in an industry uses labour to produce a variety $w \in \Omega$ of a consumption good.
- Consumers preferences for the varieties in the industry are C.E.S. with elasticity $\sigma>1$.
- For a firm, profits are increasing in productivity v, and decreasing in competition. 1/v = marginal production cost.

The model

Firm Dynamics monopolistic competition Model a la Hopenhayn (1992) (and Melitz, 2003)

- Each firm in an industry uses labour to produce a variety $w \in \Omega$ of a consumption good.
- Consumers preferences for the varieties in the industry are C.E.S. with elasticity $\sigma>1$.
- For a firm, profits are increasing in productivity v, and decreasing in competition. 1/v = marginal production cost.
- One-off fixed cost to enter S^C; Per-period fixed costs of production F; Fixed innovation cost K_i, i = innovation type.
- Innovation raises v if successful. v stochastically depreciates if no innovation (obsolescence).

- Marginal productivity at the frontier grows at the gross rate g > 1.
- Every period firms decide on innovation. They spend $K_i \ge 0$, for innovation of type $i \in \{0, 1, 2\}$

- Marginal productivity at the frontier grows at the gross rate g > 1.
- Every period firms decide on innovation. They spend $K_i \ge 0$, for innovation of type $i \in \{0, 1, 2\}$
 - i=0, no innovation. With some probability the firm keeps up with the frontier (relative productivity ν_t remains constant), otherwise ν_t depreciates at the rate g (obsolescence).

- Marginal productivity at the frontier grows at the gross rate g > 1.
- Every period firms decide on innovation. They spend $K_i \ge 0$, for innovation of type $i \in \{0, 1, 2\}$
 - i=0, no innovation. With some probability the firm keeps up with the frontier (relative productivity v_t remains constant), otherwise v_t depreciates at the rate g (obsolescence).
 - *i* = 1, incremental innovation: the firm invests to increase probability to keep up with frontier.
 - i = 2, radical innovation: small probability to make a big jump to the frontier. v_t depreciates faster if it fails.

- Marginal productivity at the frontier grows at the gross rate g > 1.
- Every period firms decide on innovation. They spend $K_i \ge 0$, for innovation of type $i \in \{0, 1, 2\}$
 - i=0, no innovation. With some probability the firm keeps up with the frontier (relative productivity ν_t remains constant), otherwise ν_t depreciates at the rate g (obsolescence).
 - *i* = 1, incremental innovation: the firm invests to increase probability to keep up with frontier.
 - i = 2, radical innovation: small probability to make a big jump to the frontier. v_t depreciates faster if it fails.
 - Innovation cost: $K_2 > K_1 > K_0 = 0$.

Timing and Financing frictions

Budget constraint:

$$a_t = R(a_{t-1} - K(I_{t-1}) - d_{t-1}) + \pi_t(v_t, \varepsilon_t)$$
 (1)

Firms need to pay in advance the fixed costs of production F
 and of innovation K:

Timing and Financing frictions

• Budget constraint:

$$a_t = R(a_{t-1} - K(I_{t-1}) - d_{t-1}) + \pi_t(v_t, \varepsilon_t)$$
 (1)

- Firms need to pay in advance the fixed costs of production F and of innovation K:
- Continuation is feasible only if:

$$a_t \ge F$$
 (2)

• Innovation is feasible only if:

$$a_t \ge F + K$$
 (3)

Value functions

we define $V_t^1(a_t, \varepsilon_t, v_t)$ as the value function today conditional on doing incremental innovation:

$$\begin{aligned} V_t^1\left(a_t, \varepsilon_t, v_t\right) &= -K(1) + \frac{1 - \delta}{R} \\ \left\{ \begin{array}{l} \xi^{\mathit{INC}} E_t\left[V_{t+1}\left(a_{t+1}, \varepsilon_{t+1}, v_t\right) + \pi_{t+1}\left(\varepsilon_{t+1}, v_t\right)\right] \\ + \left(1 - \xi^{\mathit{INC}}\right) E_t\left[V_{t+1}\left(a_{t+1}, \varepsilon_{t+1}, \frac{v_t}{g}\right) + \pi_{t+1}\left(\varepsilon_{t+1}, \frac{v_t}{g}\right)\right] \end{array} \right\} \end{aligned}$$

Then we define $V_t^2(a_t, \varepsilon_t, v_t)$ as the value function today conditional on doing radical innovation:

$$V_{t}^{2}(a_{t}, \varepsilon_{t}, v_{t}) = -K(2) + \frac{1 - \delta}{R}$$

$$\begin{cases} \xi^{I} E_{t} \left[V_{t+1}(a_{t+1}, \varepsilon_{t+1}, 1) + \pi_{t+1}(\varepsilon_{t+1}, 1) \right] \\ + \left(1 - \xi^{I} \right) E_{t} \left[V_{t+1}\left(a_{t+1}, \varepsilon_{t+1}, \frac{v_{t}}{g^{fail}} \right) + \pi_{t+1}\left(\varepsilon_{t+1}, \frac{v_{t}}{g^{fail}} \right) \right] \end{cases}$$

Value functions

And finally, the value function conditional on not innovating is:

$$V_{t}^{0}\left(a_{t},\varepsilon_{t},v_{t}\right) = \frac{1-\delta}{R}$$

$$\left\{ \begin{array}{c} \xi^{NI}E_{t}\left[V_{t+1}\left(a_{t+1},\varepsilon_{t+1},v_{t}\right) + \pi_{t+1}\left(\varepsilon_{t+1},v_{t}\right)\right] \\ + \left(1-\xi^{NI}\right)E_{t}\left[V_{t+1}\left(a_{t+1},\varepsilon_{t+1},\frac{v_{t}}{g}\right) + \pi_{t+1}\left(\varepsilon_{t+1},\frac{v_{t}}{g}\right)\right] \end{array} \right\}$$

The firm then makes the innovation decision I_t which maximizes the firms' value:

$$V_{t}^{*}\left(a_{t},\varepsilon_{t},v_{t}\right)=\operatorname*{arg\,max}_{I_{t}\in\left\{ 0,1,2\right\} }\left\{ V_{t}^{0}\left(a_{t},\varepsilon_{t},v_{t}\right),V_{t}^{1}\left(a_{t},\varepsilon_{t},v_{t}\right),V_{t}^{2}\left(a_{t},\varepsilon_{t},v_{t}\right)\right\}$$

Such that:
$$a_t \geq F + K_i$$

Given the innovation decision, the value of the firm at time t is:

$$V_{t}\left(a_{t},\varepsilon_{t},v_{t}\right)=1\left(a_{t}\geq F\right)\left\{\max\left[V_{t}^{*}\left(a_{t},\varepsilon_{t},v_{t}\right),0\right]\right\}\tag{4}$$

Entry decision

- Every period there is free entry. New potential entrants, with endowment a_0 , can learn their type v_0 after having paid an initial cost S^C .
- Once they learn their type v_0 , they decided whether or not to start activity.
- The free entry condition:

$$\int\limits_{\underline{v}}^{\overline{v}} \max \left\{ E^{\varepsilon_0} \left[V_0 \left(a_0, v_0, \varepsilon_0 \right) \right], 0 \right\} f(v_0) dv_0 - S^{\mathcal{C}} = 0 \qquad (5)$$

Calibration with risky innovation

	Matched parameters						
	Value	Moment to match	Data	Baseline sir			
δ	0.03	employment share of exiting firms	8.2%	8%			
r	1.02	average real interest rate	2%	2			
F	0.2	average ratio fixed costs/labour costs	0.3	0.23			
\overline{V}	1	normalized to 1.	n.a.	n.a.			
<u>v</u>	0.969	Cross sectional dispersion of firm average profits/added $\nu.$	0.044-0.064*	0.020			
$\mathcal{S}^{\mathcal{C}}$	0.6mean	profits/added value	0.019-0.030*	0.023			
$\frac{v}{S}^C$	0.15	average of time series vol of profits/ad.v. at the firm level	0.060-0.084*	0.052			
g	1.0035	average yearly decline in profits/sales. for a non inn. firm	3%	3%			
K^{inn}	0.05	average r&d/added value	3%	4%			
α^{not}	0.6	average age of firms	24	21			
α^{keep}	0.8	% of innovating firms (all innovation together)	47%	58%			
α^{inn}	0.1	% of firms making losses	0.46%	25%			
a 0	0.4	% of firms going bankrupt every period	0.5%	0.5%			

Intuition of the result

• Financing frictions have several effects:

Intuition of the result

- Financing frictions have several effects:
- Some young firms go bankrupt.
- Fewer firms enter
- Some young firms cannot innovate because of current or future expected financial problems.
- Older (and more wealthy) firms enjoy less competition and higher profits

Intuition of the result

- Financing frictions have several effects:
- Some young firms go bankrupt.
- Pewer firms enter
- Some young firms cannot innovate because of current or future expected financial problems.
- Older (and more wealthy) firms enjoy less competition and higher profits
 - Effects 1 to 3 reduce innovation of young firms.
 - Effect 4 encourages incremental innovation and penalizes risky innovation: essential to match life cycle dynamics.

 Empirical analysis shows that financing frictions are correlated to slower innovation growth and productivity growth along the life cycle of firms.

- Empirical analysis shows that financing frictions are correlated to slower innovation growth and productivity growth along the life cycle of firms.
- A calibrated model with heterogenous firms can replicate these dynamics if we introduce the possibility of "radical" innovation.

- Empirical analysis shows that financing frictions are correlated to slower innovation growth and productivity growth along the life cycle of firms.
- A calibrated model with heterogenous firms can replicate these dynamics if we introduce the possibility of "radical" innovation.
- The most important effect of financing frictions on innovation and aggregate productivity is the indirect competition effect.