# Debt Dynamics and Excess Sensitivity of Consumption to

Transitory Wealth Changes\*

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June 20, 2011

#### Abstract

We analyze the consumption-wealth relationship using a framework that accounts for transitory variation in wealth, and in a setting where transitory variation in household net worth is not dominated by boom and bust cycles in stock markets. We find that a transitory wealth increase anticipates a substantial transitory increase in consumption. In addition, we find that gross asset wealth and household debt are positively related. Both findings constitute departures from standard lifecycle/Permanent Income Hypothesis theory with complete financial markets.

*JEL* codes: C22, C32, E21

Keywords: Permanent Income Hypothesis, liquidity constraints,

permanent-transitory decomposition.

<sup>\*</sup>This is the pre-peer review version of the following article: De Veirman, Emmanuel and Ashley Dunstan (2012): "Debt Dynamics and the Relationship between Consumption and Cyclical Wealth Changes", *Economic Record* 88 (282), 330-340, which has been published in final form at http://onlinelibrary.wiley.com/doi/10.1111/j.1475-4932.2012.00812.x/abstract. We thank Phil Briggs, Andrew Coleman, Felix Delbrueck, Karen Dynan, Oleg Korenok, Andreas Lehnert, Thomas Lubik, Pierre-Daniel Sarte, Jirka Slacalek, as well as seminar participants at the Federal Reserve Bank of Richmond, the Banque de France, the College of William and Mary, Virginia Commonwealth University, the University of Alabama, the University of Amsterdam, the University of Leuven, and the Reserve Bank of New Zealand for comments and discussion. Any errors are our own. The views expressed in this paper are those of the authors and do not necessarily reflect the views of the Reserve Bank of New Zealand.

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## 1 Introduction

In this paper, we test two little-investigated implications of standard Permanent Income Hypothesis (PIH) theory with complete financial markets. The first implication concerns the response of consumption to transitory wealth changes, while the second pertains to the relation between household debt and household assets.

First, in standard PIH theory, a transitory wealth shock implies a small but instantaneous consumption response. The reason for the small consumption response is that a transitory wealth shock has a small effect on households' expected lifetime resources and therefore on permanent income.

However, the empirical response of consumption to transitory shocks is little-investigated. The conventional approach to estimating the consumption-wealth relation only measures the response of consumption to permanent wealth changes, and abstracts from transitory wealth changes altogether. This approach, reviewed in Davis and Palumbo (2001), consists of estimating a cointegrating relation between consumption and wealth, and to assume that any transitory deviation from the long-run relation can only be corrected for by changes in consumption.

In this paper, we investigate the effect of transitory wealth changes by applying permanenttransitory decomposition in a vector error correction framework. This framework was also applied to the consumption-wealth relation by Pichette and Tremblay (2003), Lettau and Ludvigson (2004), Chen (2006), Fernandez-Corugedo, Price and Blake (2007), Hamburg, Hoffmann and Keller (2007), and Fisher, Otto and Voss (2009).

Our paper contributes by using data for New Zealand. Unlike in Australia and the United States, stock market fluctuations explain a negligible factor of overall variation in New Zealand household net worth. The difference with Australia arises because pension savings account for a much larger share of household assets in Australia, where pension saving has been compulsory since the early 1990s.<sup>1</sup>

Because of the low share of stock market wealth in New Zealanders' porfolio, we are in a better position to shed light on the response of consumption to transitory variation in asset classes other than stocks, and to transitory variation in housing wealth in particular. In comparison, in Lettau and Ludvigson's (2004) study for the United States, short-run deviations from the longrun relationship are largely caused by transitory fluctuations in stock market wealth. Therefore, their finding that consumption does not significantly error-correct indicates that households do not appear to adjust spending much in response to transitory stock market fluctuations. But this finding still allows for the possibility that consumption responds to transitory variation in other asset classes.

We find that in New Zealand, transitory changes in wealth do anticipate substantial transitory changes in consumption. This finding is at odds with standard Permanent Income Hypothesis/lifecycle theory with complete financial markets. It is related to existing findings of 'excess sensitivity' of consumption to current income,<sup>2</sup> but is different in the sense that we explicitly characterize the transitory component of wealth and document its relation to consumer spending.

The second implication of PIH theory that we test pertains to the relation between household debt and household assets. The first implication, that permanent income consumers respond instantaneously but by a small amount to transitory wealth shocks, requires the assumption of frictionless financial markets that allow households to freely borrow more in response to a

<sup>&</sup>lt;sup>1</sup>Comparing Australian and New Zealand household survey data, Littlewood (2010) finds that in 2006, pension saving accounted for 15.9 percent of household assets in Australia, and for only 1.8 percent in New Zealand. The surveys also indicate that in almost all other respects, the household wealth composition is relatively similar in both countries.

 $<sup>^{2}</sup>$ Flavin (1981) documents that consumption responds more to current income than warranted by the information content of current income for permanent income. Campbell and Mankiw (1989) provide evidence in favor of a model where a fraction of households consume their current income rather than their permanent income.

transitory wealth decrease, and to temporarily accumulate more savings after a transitory wealth increase. This indicates that the Permanent Income Hypothesis implies a negative relationship between transitory changes in the value of gross asset holdings and changes in household debt.

This second implication is rarely examined. The macroeconomic literature on consumption wealth effects focuses on net worth without accounting separately for assets and liabilities. In this paper, we detect a positive relationship between gross asset wealth and household debt, both in terms of transitory deviations from trend as well as in the long run. Our results suggest that increases in asset prices tend to be associated with increased borrowing, a dynamic which is missing in studies that focus on household net worth. This finding is intuitive from a practitioner's point of view, but it is at odds with standard Permanent Income Hypothesis / lifecycle theory.

In our interpretation section, we argue that both the finding that transitory wealth changes anticipate a substantial transitory consumption response and that debt relates positively to changes in gross wealth are consistent with the hypothesis that a non-trivial fraction of households is subject to a binding liquidity constraint.

The remainder of our paper is structured as follows. Section 2 discusses data choices and characterizes the data. Section 3 explains the theoretical framework. Section 4 presents our empirical specification and results. Section 5 provides economic interpretation. Section 6 concludes.

### 2 Data

In this section, we first discuss our choices regarding data definitions. We then discuss the data, and document that stock market cycles do not dominate wealth variation in New Zealand. We refer to the Appendix for detailed information on data sources and the methodology used for constructing the variables. In this paper, we use aggregate New Zealand data on real per-capita total household consumption, household wealth, and after-tax labor income. All data are for the period 1990Q1-2009Q1.

As we will discuss in Section 3, any household's consumption choices are in principle influenced by its total expected lifetime resources. Lifetime resources encompass current asset net worth and human wealth.

In this paper, we split asset net worth into two separate variables: household debt and the gross value of current asset holdings. Our measure of gross asset wealth combines the aggregate value of the housing stock with the total value of financial assets.

As for human wealth, current income constitutes its observable part. Our income measure is after-tax labor income, which differs from disposable income in that it excludes property income. Labor income is the standard income measure in studies on the consumption wealth effect.<sup>3</sup> The reasoning behind using labor income is that property income is already accounted for by returns on the stock of wealth.

We use a measure of household consumption that includes spending on durable goods as well as on non-durable goods and services. This is consistent with the fact that our asset wealth measure excludes the stock of durable goods. It means that we treat the purchase of durable goods as consumption rather than as wealth accumulation.

As Rudd and Whelan (2006) emphasize, for estimating a long-run relation between consumption and wealth it is crucial to deflate all variables by the same price index. We use the Consumer Price Index (CPI) for that purpose.

We are now ready to discuss the patterns in the data. Figure 1 plots consumption and aftertax labor income. The recession of the early 1990s reflects a disinflation associated with the first

<sup>&</sup>lt;sup>3</sup>See for instance Lettau and Ludvigson (2004) and Rudd and Whelan (2006).

years of inflation targeting by the Reserve Bank of New Zealand. In the mid- and late 1990s, consumption and income grew at similar rates. Consumption grew faster than labor income in the 2000s.

Figure 2 shows household net worth and its components. The figure suggests that patterns in total net worth largely reflect changes in the value of the housing stock. This is consistent with the large share of housing in total assets. On average over our sample period, housing accounts for 68% of total household assets, which is more than double the share in the United States (31% over our sample period<sup>4</sup>). The share of housing wealth in New Zealand household assets increases from 65% in 1990 to 74% in 2009, an increase which largely reflects a housing boom between 2001 and 2007. The fact that housing wealth exerts such a large influence on developments in New Zealand household net worth implies that stock market cycles have only a minor influence on net worth.

A final point to note from Figure 2 is that the balance of outstanding household liabilities has tended to increase at a faster pace than asset worth has.

To better understand the role of stock wealth, we now turn to Figure 3. That figure decomposes household financial assets into stock wealth (labeled 'equity') and other financial assets. We define stock wealth as the sum of households' direct holdings of stocks and indirect stock holdings through financial intermediaries such as mutual funds and pension schemes.<sup>5</sup> The striking feature of Figure 3 is the comparatively small share of stock wealth in financial wealth. On average over our sample period, direct and indirect equity combined account for less than one third of financial wealth, and 9 percent of total household assets. This corresponds to the fact that the New Zealand

<sup>&</sup>lt;sup>4</sup>Both the New Zealand and the US ratios are as a share of household assets excluding durable goods. US data are from Haver.

<sup>&</sup>lt;sup>5</sup>The stock wealth series accounts for direct and indirect holdings of domestic as well as foreign stocks. It excludes assets other than stocks held through financial intermediaries.

stock market is small compared to stock markets in other OECD economies, in the sense that a comparatively small fraction of New Zealand companies are listed on the stock market. Relative to GDP, New Zealand stock market capitalization is only about one-third to one-fourth as large as in the United States, the United Kingdom and Australia.

### 3 Analytical Framework

In this section, we discuss the theoretical underpinnings of our framework for estimating the long-run relationships between consumption, gross wealth, debt and income.

There are two major ways to motivate a long-run consumption relation. The first approach implies deriving a log-linear consumption equation from the traditional consumption function according to which aggregate consumption  $C_t$  in any year t is a constant multiple m of total lifetime wealth, consisting of asset wealth  $A_t$  and human wealth  $H_t$ :

$$C_t = m \left( A_t + H_t \right) \tag{1}$$

This relationship reflects the conventional interpretation of the 'Permanent Income Hypothesis'. According to equation (1), households consume their permanent income, which is the annuity value of their lifetime resources. This equation follows from a lifecycle/Permanent Income Hypothesis model under particular assumptions. For instance, it requires that consumer choices are not influenced by uncertainty, either because households have perfect foresight about the future or because household preferences take a particular form (quadratic utility) that implies certainty equivalence. It also requires that households can freely lend and borrow in frictionless financial markets. Equation (1) also assumes that wealth returns are constant over time.<sup>6</sup>

In this paper, we refer to the perfect foresight/certainty equivalence model with frictionless financial markets as the 'standard' or 'conventional' Permanent Income Hypothesis/lifecycle model.<sup>7</sup>

A second way to motivate a long-run consumption relation is to derive it from a single equation: the intertemporal budget constraint. This is the approach we adopt in this paper. Unlike the first approach, this second approach does not impose that all households are permanent income consumers, nor does it impose the above-mentioned assumptions required to derive equation (1). Therefore, it allows for the possibility that households take uncertainty into account, for instance by saving out of precaution against adverse shocks. Similarly, the existence of an intertemporal solvency constraint neither requires nor rules out the possibility that households are liquidity constrained in terms of the amount they can borrow in any given period.

Given this level of generality, we use the log-linearized budget constraint as part of our framework for testing two implications of the conventional Permanent Income Hypothesis. First, equation (1) implies that consumption only responds to wealth changes to the extent that they affect the household's expected lifetime resources. Transitory shocks have a small effect on lifetime resources. Therefore, equation (1) implies that transitory wealth shocks have a small effect on consumption. The equation also implies that the full consumption response occurs on impact. To test these implications, this paper estimates the empirical response of consumption to transitory shocks.

<sup>&</sup>lt;sup>6</sup>See De Veirman and Dunstan (2011) for a PIH model with time-varying returns.

<sup>&</sup>lt;sup>7</sup>The Permanent Income Hypothesis is due to Friedman (1957). Modigliani and Brumberg (1954) developed the original lifecycle model, with subsequent empirical evidence by Ando and Modigliani (1963). Quadratic preferences and certainty equivalence have been a common assumption since Hall (1978). Attanasio (1999) provides a clear overview of the various incarnations of the lifecycle model. In this regard, see also Deaton (1992), Muellbauer (1994), and Davis and Palumbo (2001).

Second, the desire by households to smooth consumption in the face of mean-reverting wealth shocks implies that they temporarily accumulate savings after a transitory wealth increase, and temporarily borrow more in response to a transitory wealth decrease. This suggests a negative relationship between transitory wealth changes and household debt. To test this second implication, we extend the existing budget constraint framework in such a way that debt enters as a variable separate from gross asset wealth, and investigate the sign of the relationship between changes in assets and liabilities.

We now explain how to derive a long-run equation involving consumption, gross wealth, debt and income from the intertemporal budget constraint. In sequence, we discuss the steps carried out by Campbell and Mankiw (1989), Lettau and Ludvigson (2001), and our extension to allow for explicit debt.

Campbell and Mankiw (1989) start from an aggregate intertemporal budget constraint of the following form:

$$W_{t+1} = (1 + r_{w,t+1}) (W_t - C_t)$$
(2)

where  $W_{t+1}$  represents total lifetime resources in period t + 1,  $C_t$  represents consumption, and  $r_{w,t+1}$  is the net return on wealth. In this specification,  $W_{t+1}$  includes asset wealth and human wealth. This reflects the assumption that all wealth, including expected future labor income, in principle has a market value which can be spent on consumption. That is to say, equation (2) by itself allows for the possibility that households borrow against future labor income and spend the borrowed funds today. This is because the budget constraint is purely an intertemporal solvency condition that prevents households from borrowing more than they will ever be able to repay. However, the budget constraint can in principle co-exist with additional, more stringent

constraints on household borrowing, for instance a liquidity constraint that restricts borrowing to a fraction of current assets.

Dividing equation (2) by  $W_t$ , taking logarithms, and approximating the term  $\log(1 - \exp(c_t - w_t))$  around the steady-state log consumption-wealth ratio c - w, Campbell and Mankiw (1989) derive an accumulation equation for wealth, which decomposes wealth growth into a contribution of wealth returns and a contribution due to the fraction of wealth that is consumed in any given period:

$$\Delta w_{t+1} = r_{w,t+1} + (1 - \frac{1}{\rho})(c_t - w_t) \tag{3}$$

Lower caps denote variables in logarithms. We omit constants throughout the theoretical section. Wealth growth  $\Delta w_{t+1}$  depends on the rate of return  $r_{w,t+1} \approx \log(1 + r_{w,t+1})$ , and it depends negatively on the log ratio of current consumption to wealth  $c_t - w_t$ . The parameter  $\rho$  equals the steady-state ratio of invested wealth to total wealth. In particular,  $\rho = 1 - \exp(c - w) = [W - C]/W$ . Since the derivation assumes that there are steady-state wealth shares, it requires that wealth shares be stationary.

Re-arranging the wealth accumulation equation, solving forward, and imposing the transversality condition  $\lim_{i\to\infty} \rho^i(c_{t+i} - w_{t+i}) = 0$ , Campbell and Mankiw (1989) arrive at the equation:

$$c_t - w_t = \sum_{i=1}^{\infty} \rho^i (r_{w,t+i} - \Delta c_{t+i})$$
(4)

This equation implies that a high current ratio of consumption to wealth must be followed by high future rates of return on wealth or by low future consumption growth, else it would not be sustainable in an intertemporal sense.

Lettau and Ludvigson (2001) build on this framework. They develop equation (4) further

using three more equations, which we discuss one by one.

First, they log-linearize the wealth identity  $W_t = A_t + H_t$  to arrive at  $w_t \approx \omega \ a_t + (1 - \omega) \ h_t$ . In this equation,  $a_t$  and  $h_t$  are log asset wealth and log human wealth, respectively, and  $\omega = A/W$  is the steady-state share of asset wealth in total lifetime resources.

Second, they assume that the nonstationary component of log human wealth  $h_t$  is fully captured by log labor income  $y_t$ , which implies the assumption that discounted future labor income can be captured by a stationary term  $z_t$ . In particular, they assume that  $h_t \approx y_t + z_t$ , again omitting a constant.

Third, they assume that the rate of return on total wealth depends linearly on the return on asset wealth  $r_{a,t}$  and on human wealth  $r_{h,t}$ , with weights depending on the steady-state share  $\omega$ of asset wealth in total resources. In particular, they assume that  $r_{w,t} \approx \omega r_{a,t} + (1-\omega) r_{h,t}$ . This equation is a linear approximation of the logarithm of an accounting identity for the gross rate of return on total wealth  $1 + r_{w,t+1}$  that was first performed by Campbell (1996).

Substituting these three equations into equation (4), and taking expectations conditional on information available at time t, Lettau and Ludvigson (2001) arrive at the following equation:

$$c_t - \omega \ a_t - (1 - \omega) \ y_t = (1 - \omega) \ z_t + E_t \ \sum_{i=1}^{\infty} \rho^i (\omega \ r_{a,t+i} \ + (1 - \omega) \ r_{h,t+i} \ - \Delta c_{t+i})$$
(5)

The left-hand side of equation (5) is a log-linear combination of consumption, asset net worth, and current labor income. The right-hand side in theory involves only stationary terms: the stationary component of human wealth  $z_t$  and the expected value of a term involving future returns on asset wealth  $r_{a,t+i}$ , future returns on human wealth  $r_{h,t+i}$ , and expected future consumption growth  $\Delta c_{t+i}$ . In this paper, we extend equation (5) so as to explicitly account for the difference between debt and gross asset wealth. To do so, we log-linearize the identity  $A_t = GA_t - D_t$ , which states that asset net worth  $A_t$  equals gross asset wealth  $GA_t$  minus the stock of outstanding debt  $D_t$ . The log-linear approximation reads:

$$a_t \approx \psi \, ga_t - (\psi - 1) \, d_t \tag{6}$$

Where  $ga_t$  is log gross asset wealth and  $d_t$  is log debt.  $\psi$  indicates the steady-state ratio GA/Aof gross asset wealth to asset net worth.  $\psi$  is larger than 1 as long as steady-state debt D is positive. This implies that the coefficient  $-(\psi - 1)$  assigned to debt is negative.

Subtituting equation (6) into Lettau and Ludvigson's (2001) log-linearized wealth identity  $w_t \approx \omega \ a_t + (1 - \omega) \ h_t$ , we obtain:

$$w_t = \omega \ \psi \ ga_t - \omega \ (\psi - 1) \ d_t + (1 - \omega) \ h_t \tag{7}$$

The compound coefficients can be interpreted as follows.  $\omega \psi$  is the steady-state share GA/Wof gross asset wealth into total resources, while  $-\omega (\psi - 1)$  is the steady-state contribution D/Wof debt to total lifetime resources. This contribution is negative.

Substituting equation (7) into equation (4) along with the previously discussed assumption that current income captures the nonstationary component of human wealth, and the log-linearized equation for wealth returns, we obtain, after taking expectations:

$$c_t - (1 - \omega) y_t - \omega \psi ga_t + \omega (\psi - 1) d_t = (1 - \omega) z_t + E_t \sum_{i=1}^{\infty} \rho^i (\omega r_{a,t+i} + (1 - \omega) r_{h,t+i} - \Delta c_{t+i})$$
(8)

On the left-hand side, consumption and debt enter with a positive sign, while income and gross asset wealth enter with a negative sign. Therefore, high rates of debt affect intertemporal sustainability beyond the effect of high levels of consumption. This is because all other things equal, high debt means low net worth. As will become clear in Section 4, the difference of our empirical framework from earlier work is that it allows for the possibility that high debt levels have different implications than low levels of gross asset wealth, even if they translate into the same net worth position.

In theory, the right-hand side of equation (8) is stationary. In the next section, we will test for cointegration to examine whether there indeed exist stationary log-linear combinations of consumption, debt, gross wealth and income. If the right-hand side indeed proves to be stationary empirically, then this is in line with the assumptions that current income fully captures the nonstationary component of human wealth such that  $z_t$  is stationary, and that wealth returns are stationary. Most importantly, empirical stationarity would be in line with the hypothesis that, according to rational expectations, households believe to live in accordance with the intertemporal budget constraint. If households were to violate the intertemporal budget constraint in expectation, then the transversality condition would not hold, such that a term  $E_t \lim_{i\to\infty} \rho^i(c_{t+i} - w_{t+i}) \neq 0$  would enter the right-hand side of equation (8). If this term was non-zero, that would imply that households could only expect to be intertemporally solvent if they expect wealth (or consumption) to be infinite in the distant future.

### 4 Findings

In this section, we first specify and estimate the empirical long-run relations between consumption, gross wealth, debt, and income corresponding to equation (8). Next, we specify and estimate

our empirical model for short-run transitions towards the equilibrium relationships. Finally, we decompose variation into transitory and permanent components, and document that transitory changes in wealth predict transitory variation in consumption and borrowing. We will interpret our findings in Section 5.

#### 4.1 Long-Run Specification and Results

Table 1 presents the results from Augmented Dickey-Fuller (ADF) tests for stationarity of consumption, gross wealth, debt, and income. We enter a deterministic trend in every ADF test regression, implying that we test for the existence of a stochastic trend. For the orders of augmentation chosen by the Akaike and Schwarz information criteria, we cannot reject the null hypothesis of a unit root in either of these four variables.

Since the variables are non-stationary, we perform Johansen Trace and L-max tests for the existence of cointegration between those four variables. Table 2 documents the cointegration test results. For the purpose of the cointegration tests, we control for deterministic trends in the long-run equations. This implies that we test for the existence of common stochastic trends, but in principle allow for the variables to have different deterministic trends. The relevance of allowing for different deterministic trends will become clear later in this subsection.

The test results constitute strong evidence in favor of the existence of stochastic cointegration between consumption, gross wealth, debt and income. This suggests that households make their consumption decisions in such a way that, in expectation, they do not violate the intertemporal budget constraint.

In addition, we find that there exist two cointegrating relations in the four-variable system. This suggests that the right-hand side of (8) is best interpreted as reflecting two cointegrating residuals. Therefore, we capture the long-run links by a system of two empirical long-run equations. Identifying the two equations requires us to normalize every equation on two counts.

In the normalized system, the first equation is such that the consumption coefficient equals one, and the debt coefficient is zero. With these normalizations, we can interpret the first cointegrating relation as a consumption equation:

$$c_t - \kappa_1 - \beta_{y,1} \ y_t - \beta_{ga,1} \ ga_t = \eta_{1t}$$
(9)

In our notation,  $\kappa_1$  is a constant and  $\eta_{1t}$  is the cointegrating residual to the consumption equation. This equation differs from the usual specification in that the wealth measure  $ga_t$  is not net of liabilities. As we will see in a minute however, debt in principle relates to income and gross assets through a second cointegrating relation, and therefore plays an implicit role in the consumption equation. In the reported results, we do not enter a deterministic trend in equation (9), but the results are very similar when we do.

We now turn to the second long-run relation. In a three-variable system with consumption, net worth, and income, (unreported) L-max and Trace tests reveal the existence of a single cointegrating relationship. That is, we detect two cointegrating relations only when we decompose net worth into gross asset wealth and debt. This suggests that the second cointegrating equation captures a relationship between gross wealth and debt which is implicit in the system with net worth. Accordingly, the normalized second long-run relation has a coefficient of one on debt, and has a zero coefficient on consumption. We interpret the second cointegrating relation as a debt equation:

$$d_t - \kappa_2 - \beta_{y,2} \ y_t - \beta_{ga,2} \ ga_t - \gamma_{trend} \ t = \eta_{2t} \tag{10}$$

Where  $\kappa_2$  is a constant, t is a deterministic trend, and  $\eta_{2t}$  is the cointegrating residual for the debt equation.

Based on a likelihood ratio test, we reject the null hypothesis of no deterministic trend in equation (10) at the 1 percent significance level. This implies that debt, assets and income differ in terms of their deterministic trends in a finite sample. As we will discuss shortly, this is in line with a process of financial liberalization over the course of our sample.<sup>8</sup>

We estimate equations (9) and (10) using Dynamic OLS.<sup>9</sup>

Table 3 contains the estimated long-run coefficients. According to the consumption equation, a permanent one percent increase in gross asset wealth is associated with a permanent 0.08 percent quarterly increase in consumption. A one percent increase in income is associated with a long-run increase in consumption of 0.85 percent.<sup>10</sup>

From the debt equation, we see that permanent changes in income and gross asset wealth are positively and significantly associated with permanent changes in debt. We also find that the coefficient on the deterministic trend is positive.

As we will discuss in Section 5, the positive long-run relationship between debt and gross wealth points to the importance of financial market imperfections. Assuming that financial markets are incomplete, the presence of a positive trend in equation (10) is consistent with the interpretation that the effect of financial frictions has gradually been reduced by a trend increase in financial intermediaries' willingness to lend for any given level of current assets and income. In New Zealand,

 $<sup>^{8}</sup>$ In an open-economy model of the current account, Corsetti and Konstantinou (2009) analogously motivate including trends in an intertemporal current account equation by arguing that financial market liberalization may have induced trends in assets and liabilities, where the in-sample trend in assets may differ from the in-sample trend in liabilities.

<sup>&</sup>lt;sup>9</sup>We enter three leads and lags of the differenced log variables in the DOLS regression. We adjust standard errors for serial correlation using the procedure explained in Hayashi (2000, p. 654 ff.)

<sup>&</sup>lt;sup>10</sup>These estimates are within the range of studies for other economies. For cross-country studies in this respect, see Ludwig and Slok (2004), Case, Quigley, and Shiller (2005), and Slacalek (2009). For a panel study for Australia, see Dvornak and Kohler (2007). See also the vector error correction studies mentioned in the introduction.

banks have indeed relaxed lending standards over the course of our sample, a phenomenon that we attribute to financial liberalization and increased international financial integration.

As we are about to see in equation (11), the two long-run relations form part of a Vector Error Correction Model (VECM) for short-run dynamics. We test for stability in the long-run component of this model by computing recursive test statistics for a structural break as described in Hansen and Johansen (1999). Figure 4 documents that the test statistics never exceed the 10 percent critical value, indicating stability of the two long-run equations as well as the VECM error-correction coefficients  $\alpha$  in equation (11).

#### 4.2 Short-Run Specification and Results

Equations (9) and (10) jointly tell us how the four variables in the system relate in steady-state. In the short run, the variables will rarely exactly satisfy the long-run relations, implying that most observations for the residuals  $\eta_{1t}$  and  $\eta_{2t}$  are non-zero. Cointegration implies that such deviations from steady-state are temporary, in the sense that they tend to be corrected for by equilibriumrestoring changes in at least one of the variables in the system. We in principle allow any of the four variables of the system to correct for deviations from the long-run relations.

To do so, we estimate the following Vector Error Correction Model:

$$\Delta X_t = A_0 + A(L)\Delta X_t + \alpha \beta' \mathcal{X}_{t-1} + \varepsilon_t \tag{11}$$

where  $X_t$  is a four-by-one vector containing data on consumption, debt, income, and gross asset wealth,  $A_0$  is a vector of constants, and A(L) is a matrix polynomial in the lag operator. The five-by-one vector  $\mathcal{X}_{t-1}$  stacks the data vector with a deterministic trend:

$$\mathcal{X}_{t-1} = \begin{bmatrix} X_{t-1} \\ t \end{bmatrix}$$
(12)

The two-by-five matrix  $\beta'$  contains estimated coefficients for the two cointegrating relationships, such that:

$$\beta' \mathcal{X}_{t-1} = \begin{bmatrix} \eta_{1,t-1} \\ \eta_{2,t-1} \end{bmatrix}$$
(13)

The four-by-two matrix  $\alpha$  captures every variable's response to each of the residuals  $\eta_{1,t-1}$  and  $\eta_{2,t-1}$ . Based on the estimated adjustment parameters in  $\alpha$ , we will be able to tell whether and how strongly any variable error-corrects.  $\varepsilon_t$  is a vector of short-run residuals.

To estimate this system, we first estimate the two long-run relationships  $\beta' \mathcal{X}_{t-1}$ , storing the two cointegrating residuals, and then enter  $\beta' \mathcal{X}_{t-1}$  as a regressor as stated in equation (11). Both the Akaike Information Criterion and the Bayesian Information Criterion select a lag length of order two in a levels VAR, corresponding to a lag length of order one in the VECM. Therefore, in our case  $A(L)\Delta X_t = A_1 \ \Delta X_{t-1}$ .

Table 4 provides results. The estimated adjustment parameters on the residual  $\eta_{1,t-1}$  imply that income and gross asset wealth tend to restore their long-run relation with consumption at the 5% significance level or better, while consumption error-corrects at the 10% level. For instance, if consumption is high relative to current income and asset wealth, implying a positive value for  $\eta_{1,t-1}$ , that tends to predict rising income and asset wealth, and declining consumption. In Section 5, we provide an economic interpretation for the present section's results. Our results also show that deviations from equilibrium in the debt equation, as captured by  $\eta_{2,t-1}$ , tend to be corrected for by changes in debt and income, at the 5% level. Therefore, our model predicts that if debt is high relative to gross wealth and income, the household balance sheet position will tend to be restored through reduced borrowing and increases in income.

The coefficients on the lagged growth rates suggest that growth in asset wealth plays a key role in terms of the short-run dynamics. Growth in gross asset wealth affects all other variables significantly with a comparatively large coefficient. In addition, asset wealth growth is the only truly persistent variable in the system. Because of these two factors, the persistence in the system is primarily determined by persistence in asset wealth growth. In other words, the speed of error-correction in the system depends crucially on the persistence in the error-correction of asset wealth growth. The implications of this will become clear when we discuss impulse-responses to transitory shocks in the next subsection.

#### 4.3 Permanent-Transitory Decomposition

Cointegration implies that any deviation from the two long-run relationships is temporary, but does not imply that all variation in the individual variables is transitory. In fact, every individual variable is nonstationary and therefore contains some permanent variation. In this subsection, we disentangle the fraction of the variability in the short-run shocks  $\varepsilon_t$  that implies permanent changes in the individual variables from the fraction that implies transitory changes. We also document that transitory wealth variation predicts transitory variation in consumption and borrowing.

To decompose variation in the reduced-form VECM residuals  $\varepsilon_t$  from equation (11) into permanent and transitory components, we use a technique developed by Gonzalo and Ng (2001). Gonzalo and Ng (2001) show that, by multiplying the vector  $\varepsilon_t$  by a matrix that depends on the estimated short-run error-correction parameters  $\alpha$  as well as on the estimated long-run coefficients  $\beta$ , one obtains a set of permanent and transitory shocks  $u_t$ . Explicitly writing  $\varepsilon_t$  and  $u_t$  in terms of their entries, this means in our case:

$$\begin{bmatrix} u_{P1,t} \\ u_{P2,t} \\ u_{T1,t} \\ u_{T2,t} \end{bmatrix} = \begin{bmatrix} \alpha'_{\perp} \\ \beta \end{bmatrix} \begin{bmatrix} \varepsilon_{c,t} \\ \varepsilon_{d,t} \\ \varepsilon_{y,t} \\ \varepsilon_{ga,t} \end{bmatrix}$$
(14)

Where  $\varepsilon_{j,t}$  is the reduced-form residual to the VECM equation for the variable j, for j = c, d, y, ga. The matrix  $\alpha_{\perp}$  is orthogonal to  $\alpha$  such that  $\alpha'_{\perp}\alpha = 0$ . In our application, permanenttransitory decomposition yields two permanent shocks  $u_{P1,t}$  and  $u_{P2,t}$  and two transitory shocks  $u_{T1,t}$  and  $u_{T2,t}$ . The permanent shocks encompass any shocks that induce nonstationary variation in the variables, such as productivity shocks or permanent changes in consumer preferences. The transitory shocks explain mean-reverting fluctuations around the two long-run relationships.

The number of permanent and transitory shocks follows from the number of variables in our system as well as from the number of cointegrating relationships. We find evidence for two common stochastic trends in a four-variable system, which leaves two separate stochastic trends, each of which corresponds to one of the permanent shocks. Conversely, each of the two cointegrating relationships corresponds to one transitory shock.

The set of permanent and transitory shocks are in principle correlated. To identify the shocks, we orthogonalize the permanent and transitory shocks by applying a Cholesky decomposition to the vector  $u_t$ . As in Lettau and Ludvigson (2004), we order the permanent shocks first, implying the assumption that transitory shocks do not affect permanent shocks contemporaneously. Table 5 provides results from decomposing the variance of the forecast errors associated with the growth rates of each of the four variables into variation induced by permanent and transitory shocks.<sup>11</sup> The upper part of the table shows the fraction of transitory variation, while the lower part displays the share of permanent variation. We find that transitory variation accounts for a substantial fraction of the variation in either variable, but that overall, most variation is permanent. A crucial difference with Lettau and Ludvigson (2004) is that in our setting, there is substantial transitory variation in consumption as well as in wealth, on the order of 20 to 30 percent of total variation. This absence of a disconnect between wealth and consumption in terms of the fraction of transitory variation in principle allows for the possibility that permanent as well as transitory changes in wealth relate to consumption.<sup>12</sup>

In Subsection 4.1, we found that permanent changes in wealth are positively related to permanent changes in consumption and debt. We now investigate whether transitory variation in wealth, borrowing and spending are related. For this purpose, we produce impulse-responses from applying one-standard deviation transitory shocks to the estimated VECM from equation (11). We first consider the effect of a transitory shock associated with the long-run consumption equation before turning to the debt equation shock.

Figure 5 graphs the impulse-responses for a time-t shock to the residual of the consumption equation. The bold line reflects a Cholesky decomposition which orders the consumption equation shock before the debt equation shock. The dotted line reverses the ordering of the two transitory shocks.<sup>13</sup>

<sup>&</sup>lt;sup>11</sup>In the reported results, we do not set insignificant adjustment parameters to zero for performing the permanenttransitory decomposition. Results are very similar when we do.

 $<sup>^{12}</sup>$ As a robustness check, we also consider the case of unorthogonalized shocks. In this case, we derive correlated transitory and permanent shocks without imposing any Cholesky decomposition. Our (unreported) results suggest that our conclusions are robust to this alternative procedure. In particular, there continues to be substantial transitory as well as permanent variation in all four variables.

<sup>&</sup>lt;sup>13</sup>In both cases, we continue to order the permanent shocks before the transitory shocks.

In the case where we order the consumption equation shock before the debt equation shock, the shock to the consumption equation contemporaneously affects the debt residual. Therefore, in this case we effectively consider a shock that implies simultaneous deviations from both long-run relationships. This transitory shock is composed of time-t increases in asset wealth and income, and a time-t decrease in consumption. Because of this, the shock implies that consumption is below its long-run level as implied by current assets and income for reasons that are purely transitory.

After the shock, wealth continues to increase for two quarters, but then starts to error-correct. It does so gradually, and only reaches its pre-shock level about thirty quarters after the shock. Consumption increases in the first three quarters after the shock, but then starts to decline gradually. The dynamics of consumption track those of asset wealth with a one-quarter lag. In this respect, recall that our VECM estimates -in Table 4- imply that consumption growth strongly depends on lagged wealth growth. The impulse-responses suggest that this dependence on lagged wealth growth is a key driver of transitory consumption changes. Our finding that consumption increases substantially in response to transitory wealth changes is at odds with standard lifecycle theory, an observation which we elaborate on in Section 5.

In Figure 5, debt also tracks the dynamics of asset wealth with a lag. This finding is consistent with the estimated strong dependence of debt growth on lagged wealth growth in our VECM. It suggests that debt temporarily increases in response to transitory increases in wealth, which is equally at odds with standard lifecycle theory.

The dotted line in Figure 5 reflects a Cholesky decomposition which orders the debt equation shock before the consumption equation shock. The results are similar to the case we just discussed.

Next, consider Figure 6, which graphs the impulse-responses for a one standard deviation shock to the residual of the debt equation. As before, we consider two slightly different scenarios, differing by the ordering of the transitory shocks. The interesting feature is that wealth dynamics are different across these two experiments, which allows us to further document that transitory wealth variation is an important determinant of transitory variation in consumption and debt.

When we order the consumption equation shock before the debt equation shock (the bold line), wealth does not jump on impact, but gradually declines with respect to its steady-state growth path. In that case, wealth does not form part of the transitory shock. On the other hand, when we order the debt equation shock before the consumption shock (dotted line), wealth increases on impact.<sup>14</sup>

In the case where wealth forms part of the transitory shock, consumption and debt increase temporarily and in so doing mirror wealth dynamics with a lag, much like what we described above for Figure 5. When wealth does not jump up on impact, consumption declines more swiftly and debt rises more slowly. The reason appears to be that, with wealth declining relative to steady-state, neither consumption nor debt are pushed upward by a transitory increase in wealth.

## 5 Interpretation

In this section, we discuss that our evidence is at odds with the conventional lifecycle model, and discuss plausible explanations.

We find that consumption relates to permanent as well as to transitory wealth changes. Therefore, our results suggest that a typical wealth change matters for consumption, as long as one considers a wealth measure not dominated by stock cycles.

However, the existence of an empirical relation between consumption and wealth does not

<sup>&</sup>lt;sup>14</sup>The difference reflects the fact that in the VECM results, gross wealth barely responds to the debt equation's error-correction term. When we shock the debt equation in isolation (as in the bold line in Figure 6), this implies that wealth is a negligible part of the transitory shock.

necessarily mean that the relation is consistent with standard lifecycle theory. We now assess to which extent our results are in line with the perfect foresight/certainty equivalence lifecycle model with complete financial markets, as summarized in the consumption function (1) according to which households consume their permanent income.

Our finding that there is a positive long-run relationship between wealth and consumption is in line with the Permanent Income Hypothesis. This result is consistent with the interpretation that wealth changes cause consumption changes, even though we find that gross asset wealth and income error-correct. To see this, note that consumption can be high today relative to its longrun relation with income and wealth because households expect high future income or high future wealth returns. In this interpretation, our finding that income and wealth error-correct suggests that expectations about permanent changes in wealth or income tend to be confirmed by actual future wealth and income changes that empirically restore the long-run equilibrium relation.

However, our results are at odds with the conventional Permanent Income Hypothesis on two counts. First, the Permanent Income Hypothesis implies that consumption responds instantly, but by a small amount, to transitory wealth shocks. This implication is at odds with our finding that transitory wealth changes imply substantial transitory variation in consumption. This suggests that, while consumption plausibly depends on permanent income in the long run, short-run fluctuations in wealth cause substantial fluctuations in consumption around trend which cannot be explained by a conventional Permanent Income Hypothesis/lifecycle model. This finding is akin to findings of excess sensitivity in consumption to current income by authors including Flavin (1981) and Campbell and Mankiw (1989).

Second, we find a positive relation between household debt and gross asset wealth, a finding that the standard Permanent Income Hypothesis model with complete financial markets cannot explain. To see this, note that Permanent Income Hypothesis households who operate in complete financial markets use their ability to freely save and borrow in order to keep consumption virtually unchanged in the face of transitory shocks. To achieve this, such households temporarily increase savings in response to a transitory wealth gain, and borrow more in the event of a transitory wealth reduction. This suggests that the conventional Permanent Income Hypothesis model implies a negative relationship between transitory wealth variation and household debt. However, this theoretical implication is precisely the opposite of our empirical finding that wealth increases are associated with increases in debt.

It is outside the scope of the present paper to comprehensively evaluate alternative explanations for these two departures from traditional theory. We conjecture that as long as a model incorporates liquidity constraints on household borrowing specified in function of the current value of household assets,<sup>15</sup> it would be able to explain both the transitory responses of consumption and debt to transitory wealth changes, as well as the positive long-run relation between debt and wealth. To see this, note that an increase in collateralizable asset wealth allows liquidityconstrained households to borrow and spend more. If the wealth increase is transitory in the sense that it is later undone by a decrease in wealth, the subsequent wealth decrease will force liquidity-constrained households to borrow and spend less. Therefore, liquidity constraints appear to be in line with a hump-shaped response of consumption and borrowing to a transitory wealth increase.

<sup>&</sup>lt;sup>15</sup>In theories of consumer behavior with a credit constraint, the constraint is typically such that the value of outstanding debt cannot exceed a fraction of the current value of the housing stock. Some of these models account for household decisions over the lifetime, while others are business cycle models that restrict heterogeneity to two types of households: impatient agents who will choose to borrow, and lenders. For lifecycle models with collateral constraints, see Japelli and Pagano (1994), Ortalo-Magne and Rady (2006), Coleman (2007), and Kiyotaki, Michaelides and Nikolov (2011). For general equilibrium models with household collateral constraints, see Aoki, Proudman and Vlieghe (2004), Iacoviello (2005), Davis and Heathcote (2005), Campbell and Hercowitz (2005), Calza, Monacelli and Stracca (2007), Monacelli (2009), and Iacoviello and Neri (2010).

In our view, two alternative hypotheses provide a partial explanation in isolation (and may provide a full explanation in combination). First, households may alter spending in response to a transitory wealth shock if they mistakenly believe that it may be permanent. In isolation however, this hypothesis could not explain a rise in borrowing in response to an increase in wealth. If consumers mistakenly believe that a wealth increase is permanent but are otherwise traditional PIH consumers, they will consume a fraction of the wealth increase but save the remainder except in the last period of life.

Another partial explanation of our results lies in buffer stock saving models.<sup>16</sup> Buffer stock savers desire to converge to a particular target net worth ratio, which is consistent with our empirical finding that debt cointegrates with gross wealth and income. In isolation however, precautionary saving does not necessarily explain why consumption and debt respond to transitory wealth changes. If buffer stock savers anticipate an increase in gross wealth to be transitory, they may choose to alter consumption and borrowing very little because they expect that a subsequent decline in gross wealth will restore their net worth ratio anyway.

## 6 Conclusion

In this paper, we have documented two new empirical reasons for rejecting the implication from perfect foresight/certainty equivalence lifecycle theory with complete financial markets that all households consume their permanent income. First, we find that transitory wealth changes anticipate substantial transitory changes in consumption. Second, we detect a positive relation between debt and wealth, both in the long run and in terms of transitory variation.

<sup>&</sup>lt;sup>16</sup>For buffer stock saving models, see Zeldes (1989), Kimball (1990), Deaton (1991), Carroll (1997), Attanasio, Banks, Meghir and Weber (1999) and Gourinchas and Parker (2002). In a general equilibrium setting, see Krusell and Smith (1999).

As we discussed in the interpretation section, the hypothesis that a non-trivial fraction of households faces a binding credit constraint on current borrowing is plausibly sufficient to explain both departures from traditional consumer theory.

In this paper, we are able to document the relation between transitory wealth changes and transitory consumption changes because we not only use an empirical procedure that accounts for transitory wealth variation, but also use a measure for household net worth that is not dominated by transitory variation in stock market wealth. A natural extension of our analysis to a broader set of economies would be to examine consumption-wealth comovement after filtering the cyclical component of variation in stock market wealth from net worth.

# Tables and Figures

Figure 1: Quarterly Real Per Capita Consumption and After-Tax Labor Income



Note: This figure graphs quarterly consumption and after-tax labor income for New Zealand households, in real per capita terms. We obtained real data by deflating the nominal variables by the Consumer Price Index (CPI) with base year 2006. Further details on data construction are available in the Appendix.

Figure 2: Real Per Capita Household Net Worth and its Components



Note: This figure graphs quarterly series, in real per capita terms, for New Zealand household net worth and its subcomponents. The subcomponents are gross housing wealth, gross financial wealth, and household debt. This graph shows that fluctuations in financial wealth play a minor role in explaining fluctuations in net worth, as compared to the role played by housing wealth. We obtained real data by deflating the nominal variables by the Consumer Price Index (CPI) with base year 2006. Further details on data construction are available in the Appendix.



Figure 3: Real Per Capita Household Financial Wealth and its Components

Note: This figure graphs quarterly series, in real per capita terms, for the financial wealth of New Zealand households and its components. Equity combines households' direct holdings of stocks with indirect investments in stocks through financial intermediaries including mutual funds and pension funds. On average over the sample, the sum of direct and indirect equity is only about one third of New Zealand financial assets. We obtained real data by deflating the nominal variables by the Consumer Price Index (CPI) with base year 2006. Further details on data construction are available in the Appendix.

#### Figure 4: Long-Run Stability Tests



(Ho: this eigenvalue is stable) Tau\_t statistics for eigenvalue 1  $% \left[ 1+\frac{1}{2}\right] =0$ 

Note: This figure reports results from tests for a structural break in the long-run component of the VECM model (11) using the approach of Hansen and Johansen (1999). The top panel shows recursively computed test statistics for joint stability of the long-run consumption equation (9) and the VECM adjustment parameters to the consumption equation's error-correction term. The bottom panel shows recursive tests for the joint stability of the long-run debt equation (10) and the associated VECM adjustment parameters. Neither of the test statistics ever exceeds the 10 percent critical value. Therefore, we cannot reject the stability of the long-run component of the VECM at the 10 percent level.



Note: This figure provides the VECM impulse-responses for a one-standard deviation shock to the error-correction term corresponding to the consumption equation. We graph the variables in levels, in terms of percentage deviations from their steady-state growth path. The bold line reflects a Cholesky decomposition which orders the consumption equation shock before the debt equation shock, while the dotted line reverses the ordering of the two transitory shocks. In both cases, we find that consumption and debt increase temporarily in response to a transitory increase in wealth.



Note: This figure provides the VECM impulse-responses for a one-standard deviation shock to the error-correction term corresponding to the debt equation. We graph the variables in levels, in terms of percentage deviations from their steady-state growth path. The bold line reflects a Cholesky decomposition which orders the consumption equation shock before the debt equation shock, while the dotted line reverses the ordering of the two transitory shocks. In the former scenario, gross wealth gradually decreases with respect to steady state, while in the latter case, the transitory shock implies an upward jump in gross wealth. Consumption decreases more swiftly, and debt decreases more slowly, in the case without a wealth increase. This suggests that one of the reasons for the hump-shaped paths in consumption and debt in the other case is their response to hump-shaped wealth dynamics.

	Lag lei	ngth			
	0	1	2	3	4
Consumption	$-2.31^{S}$	-2.34	-2.28	$-2.45^{A}$	-2.62
Gross wealth	-1.64	-2.97 <sup>A,S</sup>	-2.77	-3.08	-3.11
Debt	-1.08	-1.97	$-2.61^{S}$	$-2.98^{A}$	-2.98
Income	-2.42	$-2.49^{A,S}$	-3.36*	-3.33*	-2.93
5% critical value	-3.46				

Table 1: Augmented Dickey-Fuller Tests for Stationarity

Note: Every variable is in real per capita terms. For every variable, we report the ADF test statistic for the null hypothesis that the series has a unit root. 'Lag length' refers to the order of augmentation of the testing regression. Superscripts A,S refer to the lag length selected by the Akaike and Schwarz information criteria, respectively. In every test regression, we include a constant as well as a deterministic trend. We cannot reject the null hypothesis of a unit root at the 5 percent level for any variable at any of the reported orders of augmentation. \*\*\* indicates significance at 1% level, \*\* at 5% level, and \* at 10% level.

	Lag length						
Test	$\mathrm{H}_{\mathrm{0}}$	$\mathrm{H}_A$	5% crit. value	1	2	3	4
L-max test	r=0	r=1	32.11	44.15***	52.8***	51.4***	51.1***
	r=1	r=2	25.8	28.2**	36.8***	39.5***	23.2*
	r=2	r=3	19.4	9.5	10.5	13.6	18.7*
Trace test							
	r=0	$r \ge 1$	63.7	101.1***	98.0***	107.6***	98.2***
	r=1	$\mathbf{r}{\geq}2$	42.8	39.8*	53.9***	57.3***	47.2**
	r=2	$r{\geq}3$	25.7	16.6	18.4	15.7	20.0

Table 2: Johansen L-Max and Trace Tests for Cointegration

Note: This table presents Johansen L-max and Trace test statistics for the number of cointegrating vectors in a four-variable system containing consumption, gross wealth, debt, and income. 'Lag length' refers to the number of lagged differences included in the VECM for the purpose of conducting the L-max and Trace tests. The Akaike information criterion suggests to use three lags, while the Schwarz information criterion suggests one lag. All tests include trends in the long-run relationships. For most lag specifications, we can reject the null hypotheses of no cointegration and of a single cointegrating vector, but cannot reject the null hypothesis of two cointegrating vectors, at the 5 percent level. \*\*\* indicates significance at 1% level, \*\* at 5% level, and \* at 10% level.

	consumption equation	debt equation
constant		
income	0.85***	0.50***
	(9.94)	(2.90)
gross asset wealth	0.08**	0.40***
	(2.46)	(8.19)
trend	_	0.84***
	_	(10.17)

Table 3: Estimated Long-Run Relationships

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Note: The middle column presents estimates of the long-run consumption equation (9), while the rightmost column contains the estimated coefficients of the long-run debt equation (10). We estimated both equations using Dynamic Ordinary Least Squares (DOLS) with three leads and lags of the differenced log variables. We adjusted t-statistics for serial correlation using the procedure in Hayashi (2000, p. 654 ff.). The results suggest that permanent changes in consumption and debt are positively associated with trend changes in wealth and income. \*\*\* indicates significance at 1% level, \*\* at 5% level, and \* at 10% level.

	$\Delta c_t$	$\Delta d_t$	$\Delta y_t$	$\Delta g a_t$
constant	0.03	-0.06*	0.25***	0.11*
	(0.98)	(-1.69)	(4.27)	(1.98)
$\eta_{1t-1}$	-0.11*	0.13*	0.29***	0.26**
	(-1.78)	(1.95)	(2.71)	(2.48)
$\eta_{2t-1}$	0.11**	-0.18***	0.16**	-0.004
	(2.47)	(-3.77)	(2.10)	(-0.060)
$\Delta c_{t-1}$	-0.24*	-0.14	-0.17	-0.44**
	(-1.97)	(-1.10)	(-0.83)	(-2.19)
$\Delta d_{t-1}$	0.04	-0.10	-0.32*	-0.07
	(0.37)	(-0.89)	(-1.72)	(-0.37)
$\Delta y_{t-1}$	-0.04	0.06	0.10	0.20*
	(-0.56)	(0.82)	(0.89)	(1.74)
$\Delta ga_{t-1}$	0.34***	0.37***	0.38***	0.77***
	(4.64)	(4.78)	(3.06)	(6.35)
$R^2$	0.34	0.53	0.32	0.59
$\overline{R}^2$	0.28	0.49	0.26	0.55

Table 4: Estimated Vector Error Correction Model

Note: This table reports estimates for the VECM in equation (11). t-statistics are in parentheses.  $\eta_{1t-1}$  is the error-correction term for the long-run consumption equation, while  $\eta_{2t-1}$  is the error-correction term for the long-run debt equation. The results suggest that income and gross asset wealth error-correct to the consumption equation residual at the 5 percent level or better, and that debt and income error-correct to the debt equation residual. The results also imply that lagged growth in gross wealth significantly affects growth in all four variables in the system. \*\*\* indicates significance at 1% level, \*\* at 5% level, and \* at 10% level.

	$\Delta c_{t+h} - E_t \Delta c_{t+h}$	$\Delta d_{t+h} - E_t \Delta d_{t+h}$	$\Delta y_{t+h} - E_t \Delta y_{t+h}$	$\Delta g a_{t+h} - E_t \Delta g a_{t+h}$
Transitory				
1	35.90	42.30	49.07	29.94
4	35.93	34.75	49.76	23.68
8	35.94	32.98	49.69	23.48
20	35.89	32.46	49.63	23.29
$\infty$	35.88	32.45	49.63	23.28
Permanent				
1	64.10	57.70	50.93	70.06
4	64.07	65.25	50.24	76.32
8	64.06	67.02	50.31	76.52
20	64.11	67.54	50.37	76.71
$\infty$	64.12	67.55	50.37	76.72

#### Table 5: Permanent-Transitory Decomposition

Note: For consumption, debt, income, and gross asset wealth, respectively, this table provides the fraction of the forecast error variance, in percent, explained by transitory and permanent shocks. To compute transitory and permanent shocks, we first apply the Gonzalo-Ng (2001) decomposition as stated in equation (14) to the reduced-form VECM residuals from equation (11), without setting insignificant adjustment coefficients to zero. Next, we orthogonalize the permanent and transitory shocks by applying a Cholesky decomposition to the vector of transitory and permanent shocks, assuming that transitory shocks do not contemporaneously affect permanent shocks. Unlike Lettau and Ludvigson (2004), we find that both permanent and transitory shocks account for a non-trivial part of the variation in every of the four variables.

## Appendix: Data Construction

This appendix discusses data sources and construction for consumption, net worth and income.

Our series for household consumption is from the quarterly national accounts published by Statistics New Zealand (SNZ). Household consumption excludes the consumption of private non-profit organizations. Consumption includes spending on durable and non-durable goods and services.

Household net worth is the value of the housing stock plus financial assets minus debt.

We construct a quarterly series for housing wealth from SNZ data on the total number of dwellings and the Quotable Value New Zealand (QVNZ) house price index. As an input into its house price index, QVNZ obtains capital values from local authorities which conduct periodic revaluations for the purpose of levying rates.

Our quarterly series on financial assets reflects Reserve Bank of New Zealand estimates from 1995 onwards. The Reserve Bank does not compute a quarterly series for earlier quarters. Holdings of assets other than equity evolve gradually over time, such that we construct a pre-1995 quarterly measure for each of these assets by interpolating its respective annual series with a cubic spline. To capture higher-frequency variation in stock prices, we construct a quarterly measure of direct equity holdings before 1995 by ensuring that the quarterly growth rate of the interpolated series matches the growth rate of a weighted average of the New Zealand and Australian capital price indices. At any quarter, we set the weight on the New Zealand capital price index equal to the proportion of direct equity that is domestic, while the weight for the Australian index equals the proportion of direct equity that is held abroad.

Our series for household debt reflects Reserve Bank of New Zealand estimates.

As a caveat, note that in New Zealand, measured household net worth does not include assets held in farms and other unincorporated businesses, nor assets in privately held corporations. We did not impute wealth held in unincorporated businesses and privately held firms.

We compute after-tax labor income as follows: pre-tax labor income minus tax payments plus transfer income.

SNZ produces an annual series for labor income. However, there is no directly available measure for quarterly labor income in New Zealand. We construct quarterly labor income by multiplying average hourly earnings (including overtime payments) from the Quarterly Employment Survey (QES) by hours worked from the Household Labour Force Survey (HLFS). The latter survey includes hours worked by agricultural workers and workers that are otherwise self-employed, but the former study excludes earnings of workers in those sectors. Assuming that a typical farmer or entrepreneur earns the same hourly labor income as the average hourly income in other sectors, our measure of labor income captures the compensation of employees as well as entrepreneurial income.

We construct a series of quarterly tax payments using our measure of labor income as well as data on tax rates by income bracket. For the latter, we interpolated an annual series on implied effective tax rates from SNZ's annual national accounts.

As the final input for our labor income measure, we compute a quarterly measure of transfer income. For unemployment and pension benefits, the Ministry of Social Development provides benefit rates, from which we estimated the number of beneficiaries. For other transfer receipts, there are no available estimates on benefit rates. We account for these other payments by interpolating the corresponding annual data from Work and Income New Zealand. Unlike unemployment benefits, these other payments tend to vary gradually over time, such that it is unlikely that the interpolated series omit a substantial degree of quarterly fluctuation.

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