

Discussion of
Optimal Monetary Policy with $r^ < 0$*
by Roberto Billi, Jordi Galí and Anton Nakov

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Overview

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 - 2 It can still lean against transitory shocks through full commitment, despite the permanent LT
 - 3 It can rule out sunspots by means of a nonlinear Taylor-type rule, despite the permanent LT

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 - ✓ how to talk the PS into the merits of a rule that calls for a policy-rate hike in a deflation? Learnability?

Comments: The OLG framework

- Takes the implications of demographics seriously when it comes to the labor market

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Critical (innocuous?) assumptions for isomorphism with benchmark NK model

- firms' survival rate and distribution of new equity shares

Graph

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- ✓ implications for IS equation
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- definition of intertemporal social welfare function

⇒ only considers generations alive at t

- ✓ time consistency of optimal consumption plans? (Calvo and Obstfeld, Ecma 1988)
- ✓ implicit assumption: planner's *generational*-discount factor equals agents' *time*-discount factor?
- ✓ implications for welfare-based loss function (Nisticò, JEEA 2016)

Comments: A Tractable HANK Model

Nisticò and Seccareccia (2022)

- Low-MPC Savers and high-MPC Borrowers, Idiosyncratic uncertainty
 - ⇒ Stochastic transition between types: $pr(\mathcal{B}_{t+1}|\mathcal{S}_t) = 1 - p_s$; $pr(\mathcal{S}_{t+1}|\mathcal{B}_t) = 1 - p_b$
 - ⇒ precautionary-saving and “anticipative-borrowing” motives
 - Credit frictions on the intermediary sector (leverage constraint *à la* Gertler and Karadi, 2011)
 - ⇒ Role for Unconventional Monetary Policy
- ⇒ Cyclical consumption inequality

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⇒ Cyclical consumption inequality

⇒ Steady-state real interest rate

$$r^* = -\log \beta - \log \Gamma_s \quad (1)$$

where

$$\Gamma_s \equiv p_s + (1 - p_s) U_c(\bar{C}_s)^{-1} U_c(\bar{C}_b)$$

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⇒ $r^* < 0$ if

- ✓ $\Gamma \equiv \bar{C}_s / \bar{C}_b > 1$: steady-state consumption risk for savers ⇒ $\Gamma_s > 1$: precautionary saving
- ✓ Γ and/or $1 - p_s$ large enough

Comments: A Tractable HANK Model

- With a-cyclical inequality and constant CB balance sheet \Rightarrow perfect isomorphism (BGN, 2022):

$$x_t = E_t x_{t+1} - \sigma^{-1}(i_t - E_t \pi_{t+1} - r_t^*) \quad (2)$$

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- With **cyclical inequality** and constant CB balance sheet \Rightarrow near isomorphism (Bilbiie, 2018):

$$x_t = \Phi E_t x_{t+1} - \sigma_x^{-1}(i_t - E_t \pi_{t+1} - r_t^*) \quad (3)$$

with $\Phi \equiv 1 + \delta(\chi - 1)(1 - \gamma_s)$ and $\gamma_s \equiv p_s / \Gamma_s$

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- With **cyclical inequality** and variable CB's reserves $\hat{u}_t \Rightarrow$ generalised IS schedule (NS, 2022):

$$x_t = \Phi E_t x_{t+1} - \sigma_x^{-1}(i_t - E_t \pi_{t+1} - r_t^*) - \delta E_t \Delta u_{t+1} + z^{-1} \delta (1 - \gamma_s)(E_t u_{t+1} - \bar{u}) \quad (3)$$

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✓ Transmission channels of UMP:

① "borrowing-cost channel":

savers/borrowers \Rightarrow direct effect on borrowers through long-term rate (Sims et al., REStat 2022)

② additional "idiosyncratic-risk channel":

stochastic transition ($p_s, \gamma_s < 1$) \Rightarrow direct effect on savers through precautionary saving

③ additional "cyclical-inequality channel":

counter-cyclical inequality ($\chi, \Phi > 1$) \Rightarrow GE amplification through compounding of future UMP

Equilibrium Determinacy

- Case I. a-cyclical inequality and constant CB balance sheet (BGN, 2022):

$$x_t = E_t x_{t+1} - \sigma^{-1}(i_t - E_t \pi_{t+1} - r_t^*) \quad (4)$$

$$\pi_t = \beta E_t \pi_{t+1} + \kappa x_t \quad (5)$$

$$i_t = \max\{0, r^* + \pi^* + \phi_\pi \pi_t + \phi_x x_t\} \quad (6)$$

(7)

⇒ **Determinacy condition** (Bullard and Mitra, JME 2002):

$$(1 - \beta)\phi_x + \kappa(\phi_\pi - 1) > 0$$

Equilibrium Determinacy

- Case II. cyclical inequality and constant CB balance sheet (Bilbiie, 2018):

$$x_t = \Phi E_t x_{t+1} - \sigma_x^{-1} (i_t - E_t \pi_{t+1} - r_t^*) \quad (4)$$

$$\pi_t = \beta E_t \pi_{t+1} + \kappa x_t \quad (5)$$

$$i_t = \max\{0, r^* + \pi^* + \phi_\pi \pi_t + \phi_x x_t\} \quad (6)$$

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⇒ **Determinacy condition:**

$$\sigma_x^{-1} \left[(1 - \beta) \phi_x + \kappa (\phi_\pi - 1) \right] > (1 - \beta) (\Phi - 1)$$

Equilibrium Determinacy

- Case III. cyclical inequality and variable CB's reserves (NS, 2022):

$$x_t = \Phi E_t x_{t+1} - \sigma_x^{-1} (i_t - E_t \pi_{t+1} - r_t^*) - \delta E_t \Delta u_{t+1} + z^{-1} \delta (1 - \gamma_s) (E_t u_{t+1} - \bar{u}) \quad (4)$$

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$$u_t = \bar{u} - \psi_\pi \pi_t - \psi_x x_t \quad (7)$$

⇒ **Determinacy condition:**

$$z^{-1} \delta (1 - \gamma_s) \left[(1 - \beta) \psi_x + \kappa \psi_\pi \right] + \sigma_x^{-1} \left[(1 - \beta) \phi_x + \kappa (\phi_\pi - 1) \right] > (1 - \beta) (\Phi - 1)$$

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⇒ Taylor Principle not necessary for determinacy, if UMP active enough

- ✓ Local determinacy even under **permanent liquidity trap** if UMP appropriately specified:

$$z^{-1} \delta (1 - \gamma_s) \left[(1 - \beta) \psi_x + \kappa \psi_\pi \right] > \sigma_x^{-1} \kappa + (1 - \beta) (\Phi - 1)$$

Transition paths: the benchmark NK model

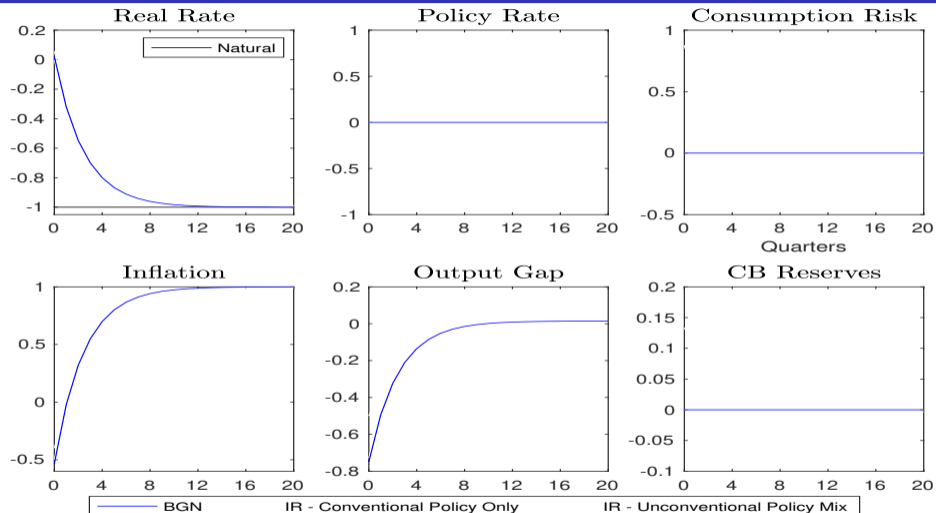


Figure: BGN: no idiosyncratic uncertainty, no UMP

Transition paths: the “conventional” THANK model

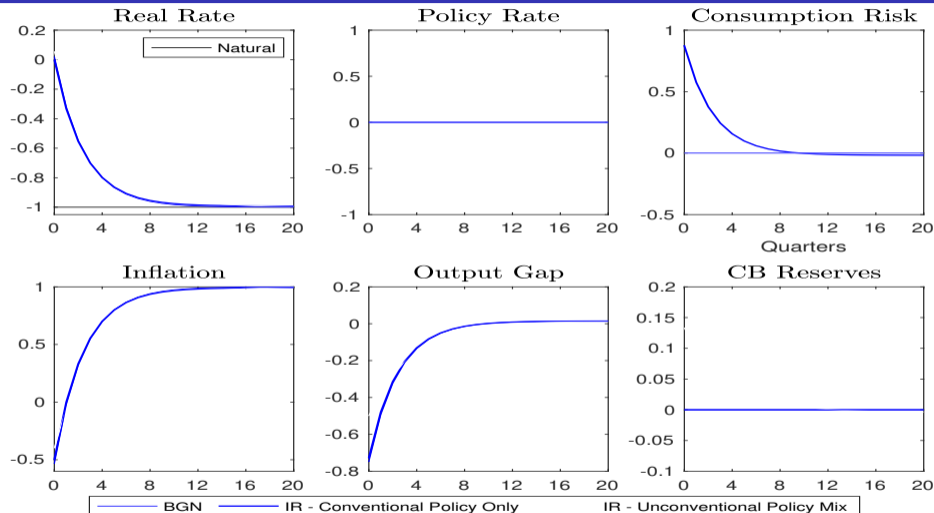


Figure: Idiosyncratic uncertainty, no UMP

Transition paths: the “unconventional” THANK model

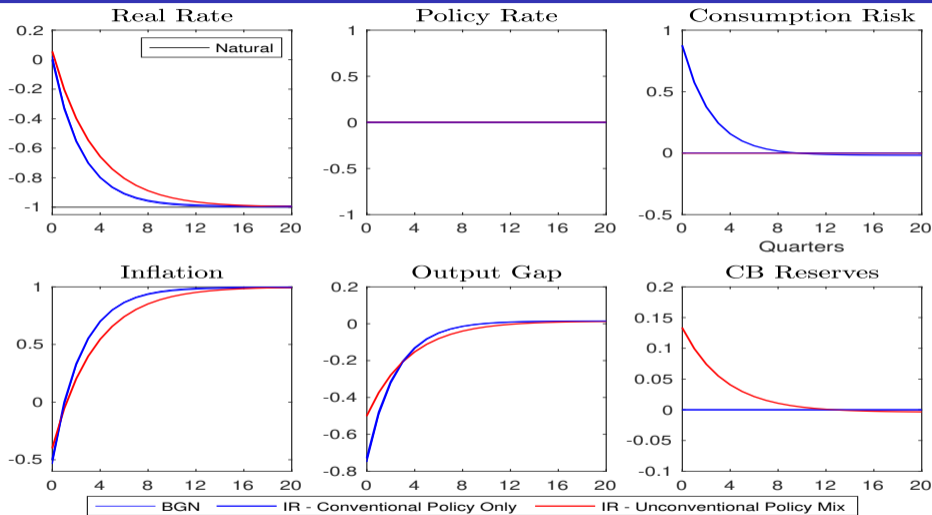


Figure: UMP shuts down idiosyncratic-risk channel \Rightarrow more gradual and less costly transition to higher $\bar{\pi}$

Stochastic simulations: the benchmark NK model

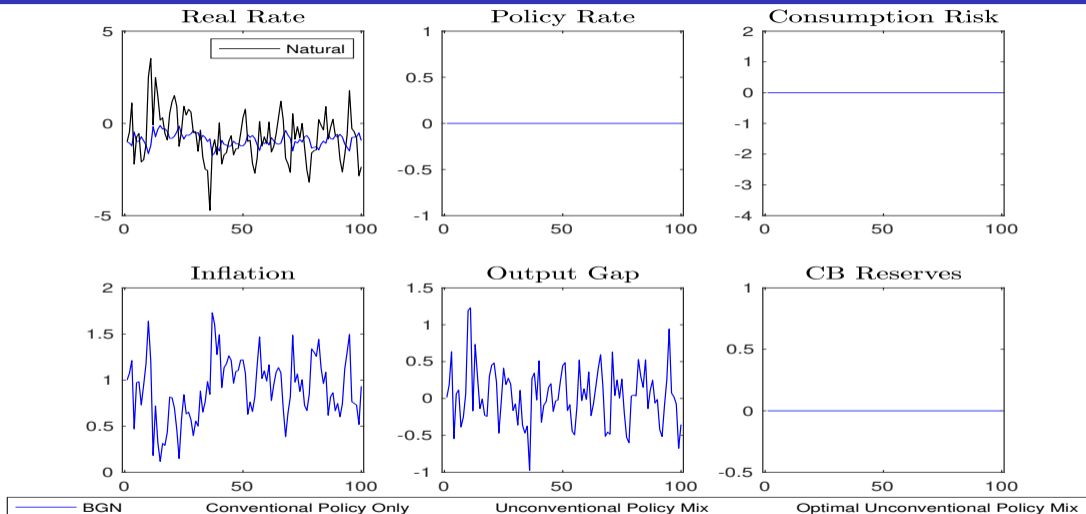


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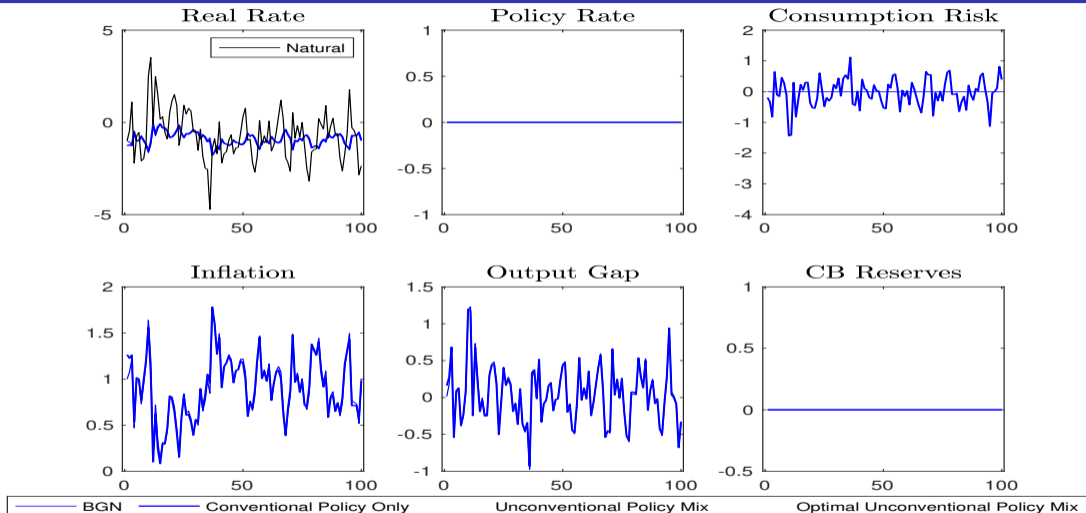


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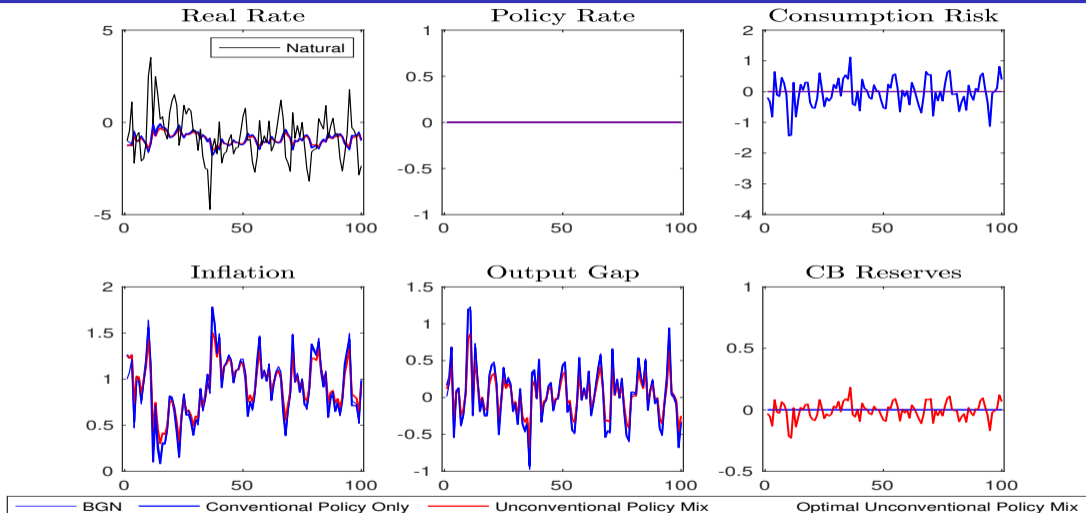


Figure: UMP shuts down idiosyncratic-risk channel \Rightarrow $\text{std}(\pi) \downarrow 22\%$ $\text{std}(x) \downarrow 32\%$

Stochastic simulations: the “unconventional” THANK model

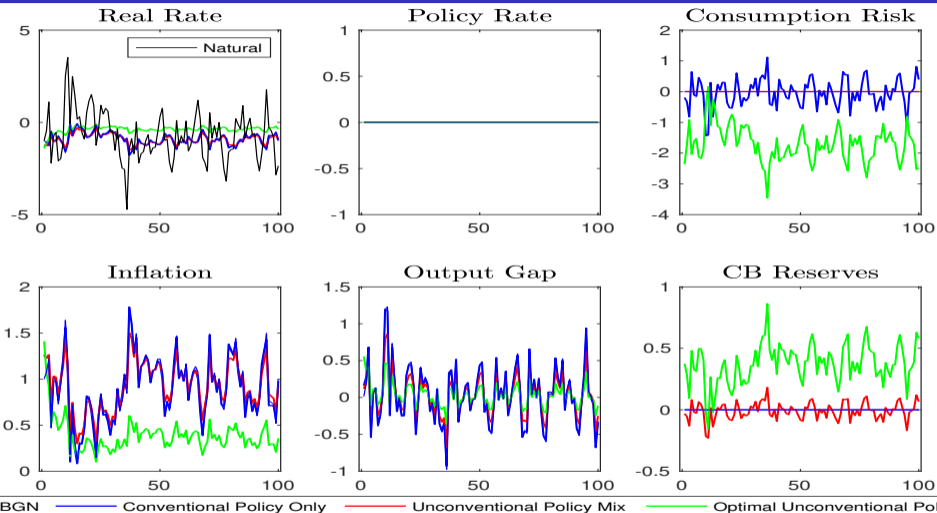
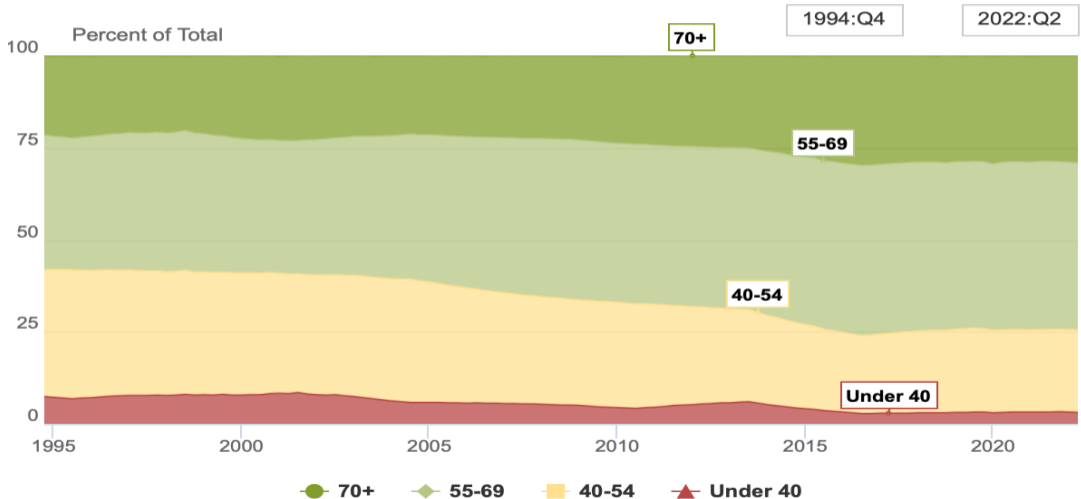


Figure: welfare maximising policy mix $\Rightarrow \bar{\pi} < 1\%$ $\text{std}(\pi) \downarrow 47\%$ $\text{std}(x) \downarrow 59\%$

- Awesome paper: very insightful
- Communicability of the policy rule; learnability of the resulting equilibrium
- What underlying economic environment?
- A role for unconventional monetary policy?

Corporate equities and mutual fund shares by age



Source: Survey of Consumer Finances and Financial Accounts of the United States