

# Unwinding Quantitative Easing: State Dependency and Household Heterogeneity

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- Monetary policy **normalization**: CB balance sheet reduction
  - Need to create sufficient **scope for monetary stimulus** against future shocks
- **Lack of evidence** on Quantitative Tightening (**QT**)
  - Study it theoretically
- **Debate on timing** of unwinding Quantitative Easing (**QE**)
  - **Raising** policy rates or **unwinding** stocks of asset purchases: what comes first?
- Idea of **state dependency**
  - Effectiveness of (unwinding) QE might be linked to the **state of the economy / financial markets**

## Research focus

- Study macroeconomic **effects of state dependency** of QE/QT
  - Different states through existence of occasionally binding **ZLB**
- Study **interaction** of state dependency **with household heterogeneity**

## Approach

- Tractable **New Keynesian model** with borrowers and savers, two types of bonds, and two monetary policy instruments
  - QE/QT operates via **portfolio rebalancing** between government bonds
  - Simulations for shocks at, close to, and above the ZLB

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**Quantitative Tightening** = *active* asset sales to the secondary market

- In or close to liquidity trap, central bank can *minimize economic costs* of MP normalization by *raising policy rate* prior to unwinding QE
  - Short-term real rate increase depresses aggregate demand
- *Asymmetry* between (absolute) effects of state-dependent QE and QT
- *HH heterogeneity* does *not* amplify QE/QT per se, but *amplifies asymmetry* *when* combined with state dependency
  - Borrowers more exposed through *direct* (portfolio) and *indirect* (wage) *effects*

- **Borrowers and Savers – TANK:** Eggertsson and Krugman (2012), Bilbiie, Monacelli, and Perotti (2013)
- **QE in RANK:** Chen, Cúrdia, and Ferrero (2012), Harrison (2012), Gertler and Karadi (2013), Harrison (2017), Harrison, Seneca, and Waldron (2021), Sims and Wu (2021)
- **QE in HANK:** Cui and Sterk (2021), Nisticò and Seccareccia (2022), Sims, Wu, and Zhang (2022a), Sims, Wu, and Zhang (2022b), Wu and Xie (2022)
- **QT:** Wen (2014), Cui and Sterk (2021), Karadi and Nakov (2021), Benigno and Benigno (2022), Sims et al. (2022a), Wei (2022), Airaudo (2023)
- **State dependency:** Haldane, Roberts-Sklar, Wieladek, and Young (2016), Bailey, Bridges, Harrison, Jones, and Mankodi (2020), Vlieghe (2021)

Model

## Two-agent New Keynesian DSGE model (**TANK-BS**)

### ↪ **Households:**

- Two types: **Borrowers** (debt-constrained, impatient) and **Savers** (RA type)
- Consume, work, save/borrow, earn labor and profit income, pay taxes [▶ More](#)
- Access to short- and long-term bonds, s.t. (portfolio) adjustment cost [▶ More](#)
  - Friction creates a wedge between bond returns
- **Portfolio balance channel:**  $QE/QT \Rightarrow \Delta$  relative asset supply  $\Rightarrow \Delta$  relative asset prices and returns  $\Rightarrow$  rebalance



- ↪ **Firms:** standard NK setting, nominal frictions (Rotemberg) [▶ More](#)
- ↪ **Government:** issues bonds, levies taxes, redistributive policies [▶ More](#)
- ↪ **Monetary authority:** Two policy tools
  - Policy rate: Conventional interest rate setting (Taylor rule)
  - Asset market operations: Buy/sell fraction of total long-term bonds

[▶ Market Clearing](#)[▶ Model](#)[▶ Calibration](#)

# Simulations

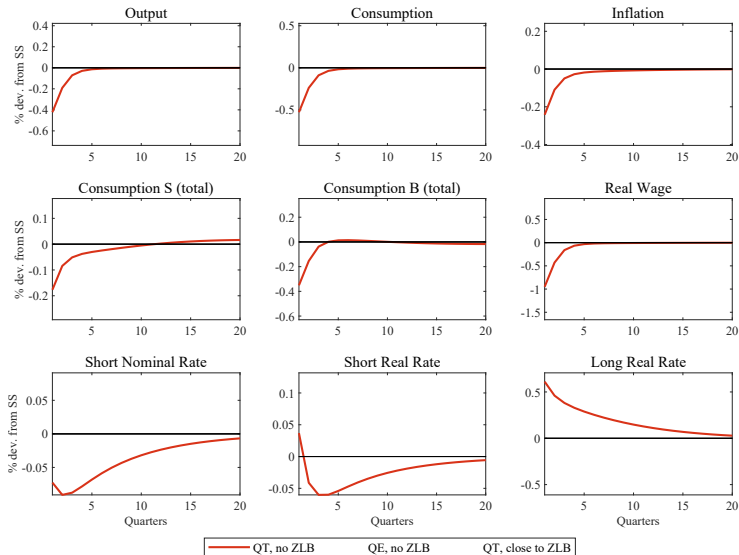
Central bank purchases/sells long-term bonds  
worth **1% of (annualized) GDP**

- Target: U.S. evidence on the peak impact of an asset purchase on real output  
→ Weale and Wieladek (2016): 0.58%

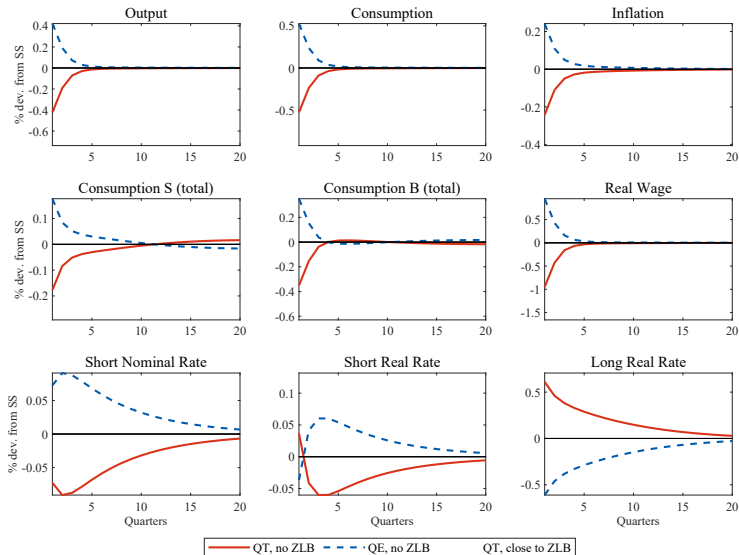
Different states of the economy:

- ① Off the ZLB: Nominal interest rate unconstrained
- ② Close to ZLB: Contractionary shock pushes economy into liquidity trap

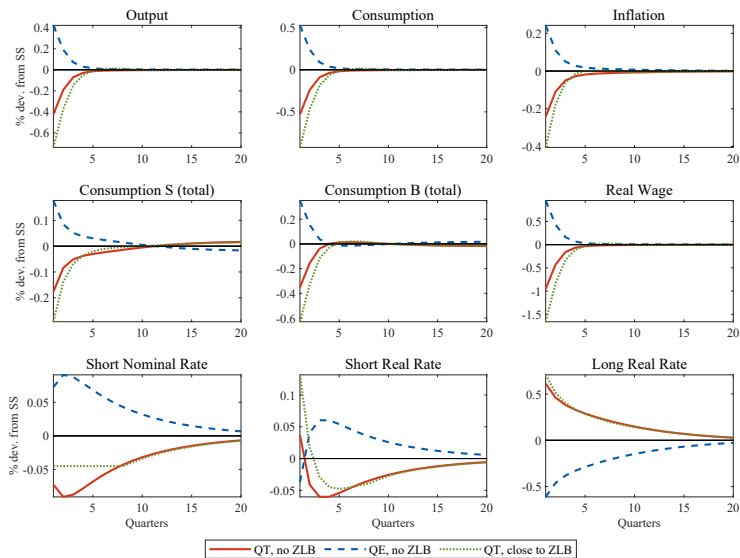
# Macroeconomic impact of unwinding QE



# Symmetric effects away from the ZLB



# What if the economy is close to the ZLB?



*When* should central banks unwind?

- First **normalize policy rate** before starting active asset sales
  - minimizes the economic costs associated with MP normalization
- To prevent that tightening brings the policy rate back to zero
  - Timing and pace: **avoid** “too early”, “too big”, and “too fast”

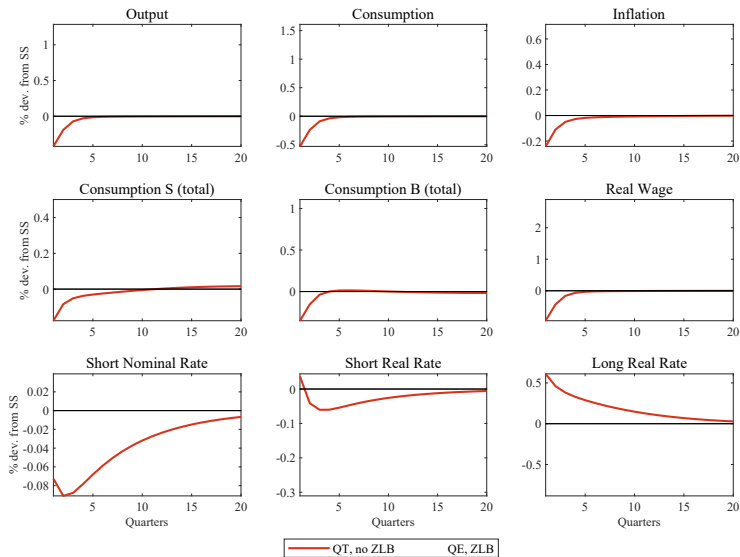
Compare **QE and QT of similar size** across different states of the economy and “quantify” the **asymmetry** coming from the ZLB

Two independent cases:

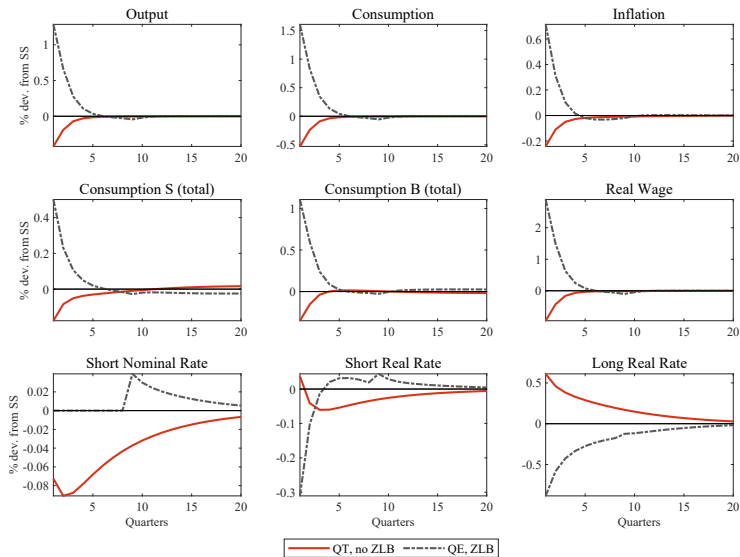
- ① QE at the ZLB → capturing US-QE1 program
- ② QT off the ZLB → US-QT1 scenario



# State-dependent asset market operations



# State-dependent asset market operations



## Net impact of QE (at ZLB) vs. QT (off ZLB)

	<b>Output</b>		<b>Inflation</b>		<b>Consumption</b>	
	QE	QT	QE	QT	QE	QT
RANK	1.05	-0.44	0.70	-0.32	1.32	-0.56
TANK-BS	1.29	-0.42	0.71	-0.24	1.61	-0.53

Multipliers on impact (baseline, in %)

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Multipliers on impact (baseline, in %)

- Asymmetry at **aggregate** level (*within* model):  $|\text{QE impact}| > |\text{QT impact}|$
- Macro effects of QE are stronger: 2x (RANK) and 3x (TANK-BS)
  - Important role of ZLB (state dependency)

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  - Macro effects of QE are stronger: 2x (RANK) and 3x (TANK-BS)
  - Important role of ZLB (state dependency)
- **Distribution** matters (*across* models):  $|\Delta\text{QE impact}| > |\Delta\text{QT impact}|$ 
  - No ZLB: relative contribution of S ↓ but high-MPC B's labor income ↑
  - With ZLB: B's labor income ↑↑ (via direct and indirect effects)

► More

► irfs QT

► irfs QE

► Robust

## Concluding Remarks

- QE as **powerful** monetary policy tool **at the ZLB** (“*temporary* substitute”)
  - **Constrained households** accelerate the stabilization of the economy
- Away from ZLB, asset market operations relatively less influential
  - Different state of the world and “complementarity” with policy rate
  - **RANK** may provide an **adequate approximation** of aggregate QE/QT effects
- At least **two scenarios**:
  - ① Strong PB channel: large macroeconomic costs or policy rate cut?
  - ② Weak PB channel and/or forceful other channels: degree of strength?

## Key take-aways

- Built a **tractable borrower-saver model** to study macroeconomic implications of doing QE and unwinding it
  - Highlighted the role of an **occasionally binding ZLB** in determining an **asymmetry** between QE and QT (state dependency)
  - When economy is close to or at ZLB, central bank should **prioritize raising** the nominal **interest rate** before unwinding QE
  - Asymmetry is **more pronounced** with **household heterogeneity** *on top*
- ⇒ **QT in practice**: state of economy, timing, pace, and channels matter



Thank you for your attention

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– Appendix –



Period utility function for  $j = \{B, S\}$

$$U(c_t^j, N_t^j) = \theta_t \left( \frac{(c_t^j)^{1-\frac{1}{\sigma}}}{1-\frac{1}{\sigma}} - \zeta^j \frac{(N_t^j)^{1+\varphi}}{1+\varphi} \right)$$

Savers ( $S$ ): Maximize lifetime utility subject to real budget constraint

$$c_t^S + b_t^S + b_t^{S,L} = r_{t-1} b_{t-1}^S + r_t^L b_{t-1}^{S,L} + w_t N_t^S + \frac{1-\tau^D}{1-\lambda} d_t - t_t - \psi_t^S - \frac{tr}{1-\lambda}$$

Borrowers ( $B$ ): Less patient than savers (value future less):  $\beta^S > \beta^B$

- Difference in discount factors induces lending from  $S$  to  $B$  in equilibrium
- Budget and borrowing constraint, with exogenous borrowing limit  $\bar{D} \geq 0$

$$\begin{aligned} c_t^B + b_t^B + b_t^{B,L} &\leq r_{t-1} b_{t-1}^B + r_t^L b_{t-1}^{B,L} + w_t N_t^B + \frac{\tau^D}{\lambda} d_t - t_t - \psi_t^B + \frac{tr}{\lambda} \\ -b_t^B - b_t^{B,L} &\leq \bar{D} \end{aligned}$$

## Households: Optimality conditions

For  $j = \{B, S\}$

$$w_t = \zeta^j (N_t^j)^\varphi (c_t^j)^{\frac{1}{\sigma}}$$

$$1 = \beta^j R_t \mathbb{E}_t \left[ \frac{\theta_{t+1}}{\theta_t} \left( \frac{c_{t+1}^j}{c_t^j} \right)^{-\frac{1}{\sigma}} \frac{1}{\Pi_{t+1}} \right] - \frac{\nu \delta}{b_t^{j,L}} \left( \delta \frac{b_t^j}{b_t^{j,L}} - 1 \right) + \mathbb{I}^j \psi_t^B$$

$$1 = \beta^j \mathbb{E}_t \left[ \frac{\theta_{t+1}}{\theta_t} \left( \frac{c_{t+1}^j}{c_t^j} \right)^{-\frac{1}{\sigma}} \frac{R_{t+1}^L}{\Pi_{t+1}} \right] + \frac{\nu \delta b_t^j}{(b_t^{j,L})^2} \left( \delta \frac{b_t^j}{b_t^{j,L}} - 1 \right) + \mathbb{I}^j \psi_t^B$$

$$0 = \mathbb{I}^j \psi_t^B \left( b_t^B + b_t^{B,L} + \bar{D} \right)$$

where  $\mathbb{I}^j$  is an indicator function with values  $\mathbb{I}^S = 0$  and  $\mathbb{I}^B = 1$ , and  $\psi_t^B \geq 0$  is the Lagrangian multiplier on the borrowing constraint.

# Long-term bonds

- Perpetuities with exponentially declining coupon ([Woodford, 2001](#))
- Bond issued at  $t$  pays  $k + 1$  periods later a nominal coupon  $\chi^k$  ( $k \geq 0$ )
- Nominal value of a bond...
  - issued at  $t$ :  $V_t$
  - issued  $k$  periods ago:  $\chi^k V_t$
- Nominal value of long-term bond holdings of  $j = \{B, S\}$ :  $B_t^{j,L} = V_t \tilde{B}_t^{j,L}$
- (Ex-post) nominal return on long-term bonds ([Harrison, 2017](#)):

$$R_t^L = \frac{1 + \chi V_t}{V_{t-1}}$$

Costly changes in asset allocation between short-term and long-term bonds  
(Chen et al., 2012; Harrison, 2017)

$$\psi_t^j = \frac{\nu}{2} \left( \delta^j \frac{b_t^j}{b_t^{j,L}} - 1 \right)^2$$

with  $\delta^j = \frac{b^{j,L}}{b^j}$

- Creates role for QE/QT as a policy instrument
- **Portfolio balance channel:** QE/QT  $\Rightarrow \Delta$  relative asset supply  $\Rightarrow \Delta$  relative asset prices and returns  $\Rightarrow$  rebalance
  - Evidence (UK): Christensen and Rudebusch (2012); Joyce, Lasaosa, Stevens, and Tong (2011)
- Rationale: imperfect substitutability between assets along yield curve  
(Andrés, López-Salido, & Nelson, 2004; Vayanos & Vila, 2009, 2021)

## Final goods producer (perfectly competitive)

- Aggregates differentiated intermediate goods (CES production function)

## Intermediate goods producers (monopolistically competitive)

- Use technology  $y_t(i) = z_t N_t(i)$  to produce varieties  $i$
- Set prices s.t. quadratic adjustment cost (Rotemberg)
- Marginal cost pricing  $\Rightarrow$  zero-profit steady state
- Phillips curve:

$$\phi_p (\Pi_t - 1) \Pi_t = \beta \mathbb{E}_t \left[ \frac{\theta_{t+1}}{\theta_t} \left( \frac{c_{t+1}^S}{c_t^S} \right)^{-\frac{1}{\sigma}} \phi_p (\Pi_{t+1} - 1) \Pi_{t+1} \frac{y_{t+1}}{y_t} \right] + \epsilon m c_t + (1 + \tau^S) (1 - \epsilon)$$

## Government budget constraint

$$b_t + b_t^L = r_{t-1} b_{t-1} + r_t^L b_{t-1}^L + \Omega_t + g_t - t_t$$

- Supply of long-term bonds and govt spending: AR(1) process
- Lump-sum taxes:  $\frac{t_t}{t} = \left(\frac{t_{t-1}}{t}\right)^{\rho^{\tau,t}} \left(\frac{b_t + b_t^L}{b + b^L}\right)^{\rho^{\tau,b}} \left(\frac{g_t}{g}\right)^{\rho^{\tau,g}}$
- Net purchases of long-term bonds by central bank:  $\Omega_t = b_t^{CB,L} - r_t^L b_{t-1}^{CB,L}$

## Monetary policy instruments

- (i) Asset purchases via fraction of total market value of long bonds ( $\sim$ AR(1)):

$$b_t^{CB,L} = q_t b_t^L$$

- (ii) Conventional interest rate setting according to Taylor rule

# Aggregation and market clearing

- Aggregate consumption and aggregate:

$$c_t = \lambda c_t^H + (1 - \lambda) c_t^S$$
$$N_t = \lambda N_t^H + (1 - \lambda) N_t^S$$

- Bond markets clearing:

$$b_t = \lambda b_t^B + (1 - \lambda) b_t^S$$
$$b_t^L = \underbrace{\lambda b_t^{B,L} + (1 - \lambda) b_t^{S,L}}_{b_t^{H,L}} + b_t^{CB,L}$$

- Resource constraint:

$$y_t = c_t + g_t + \frac{\phi_p}{2} (\Pi_t - 1)^2 y_t$$

# Model summary (1)

Labor supply	$w_t = \zeta^j (N_t^j)^\varphi (c_t^j)^{1/\sigma}, \quad j = \{B, S\}$
Euler short bonds, $S$	$1 = \beta^S \mathbb{E}_t \left[ \frac{\theta_{t+1}}{\theta_t} \left( \frac{c_{t+1}^S}{c_t^S} \right)^{-\frac{1}{\sigma}} \frac{R_t}{\Pi_{t+1}} \right] - \frac{\nu \delta^S}{b_t^{S,L}} \left( \delta^S \frac{b_t^S}{b_t^{S,L}} - 1 \right)$
Euler long bonds, $S$	$1 = \beta^S \mathbb{E}_t \left[ \frac{\theta_{t+1}}{\theta_t} \left( \frac{c_{t+1}^S}{c_t^S} \right)^{-\frac{1}{\sigma}} \frac{R_{t+1}^L}{\Pi_{t+1}} \right] + \frac{\nu \delta^S b_t^S}{(b_t^{S,L})^2} \left( \delta^S \frac{b_t^S}{b_t^{S,L}} - 1 \right)$
Budget constraint, $S$	$c_t^S + b_t^S + b_t^{S,L} = r_{t-1} b_{t-1}^S + r_t^L b_{t-1}^{S,L} + w_t N_t^S + \frac{1-\tau^D}{1-\lambda} d_t - t_t - \psi_t^S - \frac{tr}{1-\lambda}$
Euler short bonds, $B$	$1 = \beta^B \mathbb{E}_t \left[ \frac{\theta_{t+1}}{\theta_t} \left( \frac{c_{t+1}^B}{c_t^B} \right)^{-\frac{1}{\sigma}} \frac{R_t}{\Pi_{t+1}} \right] - \frac{\nu \delta^B}{b_t^{B,L}} \left( \delta^B \frac{b_t^B}{b_t^{B,L}} - 1 \right) + \psi_t^B$
Euler long bonds, $B$	$1 = \beta^B \mathbb{E}_t \left[ \frac{\theta_{t+1}}{\theta_t} \left( \frac{c_{t+1}^B}{c_t^B} \right)^{-\frac{1}{\sigma}} \frac{R_{t+1}^L}{\Pi_{t+1}} \right] + \frac{\nu \delta^B b_t^B}{(b_t^{B,L})^2} \left( \delta^B \frac{b_t^B}{b_t^{B,L}} - 1 \right) + \psi_t^B$
Budget constraint, $B$	$c_t^B + b_t^B + b_t^{B,L} = r_{t-1} b_{t-1}^B + r_t^L b_{t-1}^{B,L} + w_t N_t^B + \frac{\tau^D}{\lambda} d_t - t_t - \psi_t^B + \frac{tr}{\lambda}$
Borrowing constraint	$-b_t^B - b_t^{B,L} \leq \bar{D}$
Portfolio adj. cost	$\Psi_t^j = \frac{\nu}{2} \left( \delta^j \frac{b_t^j}{b_t^{j,L}} - 1 \right)^2, \quad j = \{B, S\}$



## Model summary (2)

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Labor demand	$w_t = mc_t \frac{y_t}{N_t}$
Production function	$y_t = z_t N_t$
Profits, aggregate	$d_t = \left[ 1 - mc_t - \frac{\phi_p}{2} (\Pi_t - 1)^2 \right] y_t$ $\phi_p (\Pi_t - 1) \Pi_t = \epsilon mc_t + (1 + \tau^S) (1 - \epsilon)$
Phillips curve	$+ \beta \mathbb{E}_t \left[ \frac{\theta_{t+1}}{\theta_t} \left( \frac{c_{t+1}^S}{c_t^S} \right)^{-\frac{1}{\sigma}} \phi_p (\Pi_{t+1} - 1) \Pi_{t+1} \frac{y_{t+1}}{y_t} \right]$
Government budget constraint	$b_t + b_t^L = r_{t-1} b_{t-1} + r_t^L b_{t-1}^L + \Omega_t + g_t - t_t$
Real short-term interest rate	$r_t = \frac{R_t}{\mathbb{E}_t \Pi_{t+1}}$
Nominal long-term bond return	$R_t^L = \frac{1 + \chi}{V_{t-1}} V_t$
Real long-term bond return	$r_t^L = \frac{R_t^L}{\Pi_t}$
Net bond purchases, $CB$	$\Omega_t = b_t^{CB,L} - r_t^L b_{t-1}^{CB,L}$
Value bond purchases, $CB$	$b_t^{CB,L} = q_t b_t^L$

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## Model summary (3)

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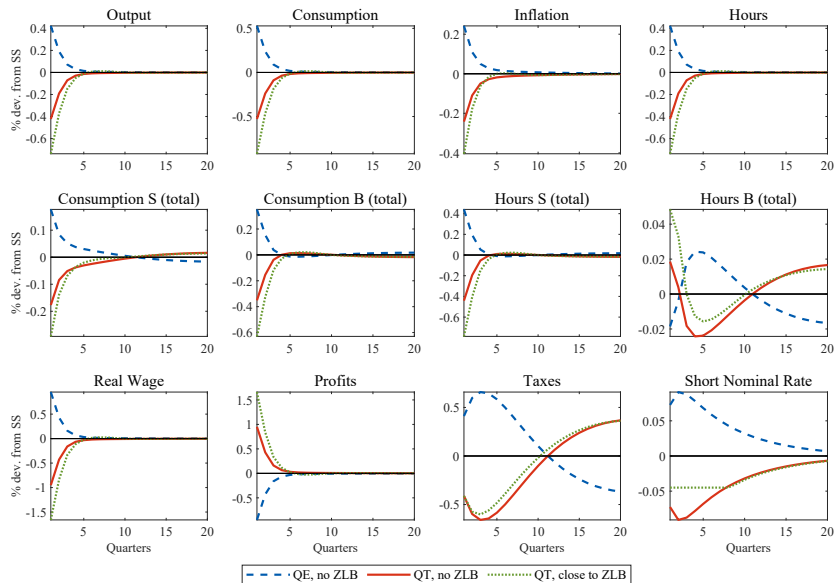
Taylor rule	$\log \left( \frac{R_t}{R} \right) = \rho_r \log \left( \frac{R_{t-1}}{R} \right) + (1 - \rho_r) \left[ \phi_\pi \log \left( \frac{\Pi_t}{\Pi} \right) \right] + \epsilon_t^m$
QE shock rule	$\log \left( \frac{q_t}{q} \right) = \rho_q \log \left( \frac{q_{t-1}}{q} \right) + \epsilon_t^q$
Fiscal rule	$\frac{t_t}{t} = \left( \frac{t_{t-1}}{t} \right)^{\rho^{\tau, t}} \left( \frac{b_t + b_t^L}{b + b^L} \right)^{\rho^{\tau, b}} \left( \frac{g_t}{g} \right)^{\rho^{\tau, g}}$
Aggregate consumption	$c_t = \lambda c_t^H + (1 - \lambda) c_t^S$
Aggregate labor	$N_t = \lambda N_t^H + (1 - \lambda) N_t^S$
Short-term bonds market clearing	$b_t = \lambda b_t^B + (1 - \lambda) b_t^S$
Long-term bonds market clearing	$b_t^L = \left( \lambda b_t^{B, L} + (1 - \lambda) b_t^{S, L} \right) + b_t^{CB, L}$
Resource constraint	$y_t = c_t + g_t + \frac{\phi_p}{2} (\Pi_t - 1)^2 y_t$
Other shock rules	$\log \left( \frac{x_t}{x} \right) = \rho_x \log \left( \frac{x_{t-1}}{x} \right) + \epsilon_t^x, \quad x = \{g, b^L, z, \theta\}$

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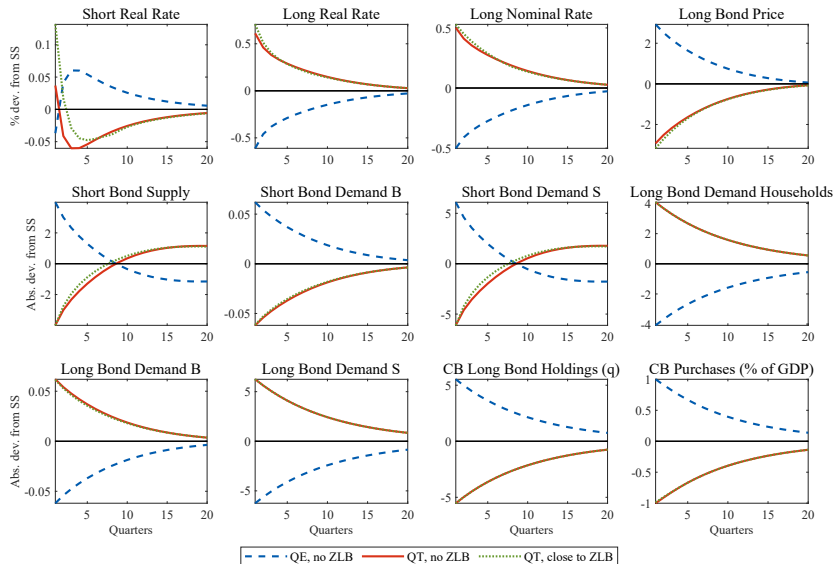
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Parameter	Description	Value
$\lambda$	Proportion of borrowers	0.35
$\sigma$	Intertemporal elasticity of substitution	1
$1/\varphi$	Frisch elasticity of labor supply	1
$\beta^S$	Discount factor, saver	0.99   0.999
$\beta^B$	Discount factor, borrower	0.95
$\bar{D}$	Borrowing limit	0.5
$\epsilon$	Elasticity of substitution between goods	6
$\phi_p$	Rotemberg price adjustment cost	42.68
$\phi_\pi$	Taylor rule coefficient on inflation	1.5
$\chi$	Long-term bond coupon decay rate	0.975
$\nu$	Portfolio share adjustment cost	0.1
$b^L/b$	Steady-state ratio of long-term to short-term bonds	0.3
$q$	Steady-state CB long-term bond holdings	0.25
$g/y$	Steady-state government-spending-to-GDP ratio	0.2
$(b + b^L)/y$	Steady-state total-debt-to-GDP ratio	0.6
$\rho^{\tau,t}$	Tax smoothing in fiscal rule	0.7
$\rho^{\tau,b}$	Tax response to total debt	0.33
$\rho^{\tau,g}$	Tax response to government spending	0.1
$\rho_q$	QE smoothing	0.9

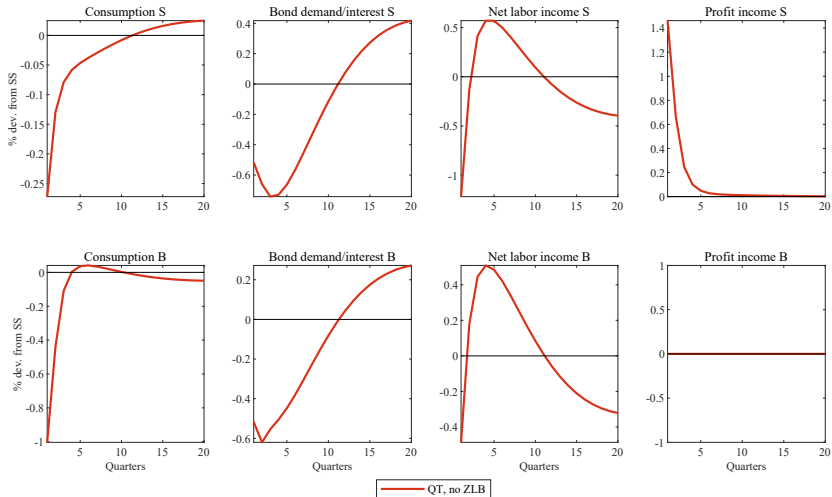
# QE/QT shock and QT shock near the ZLB (1/2)



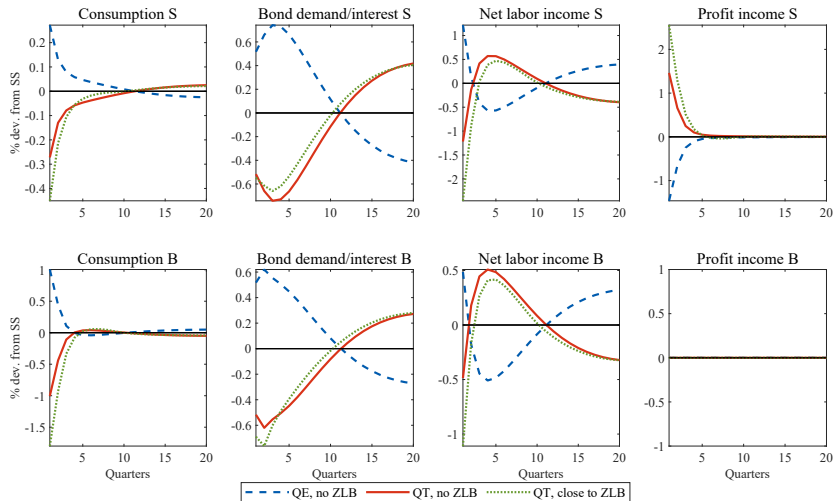
# QE/QT shock and QT shock near the ZLB (2/2)



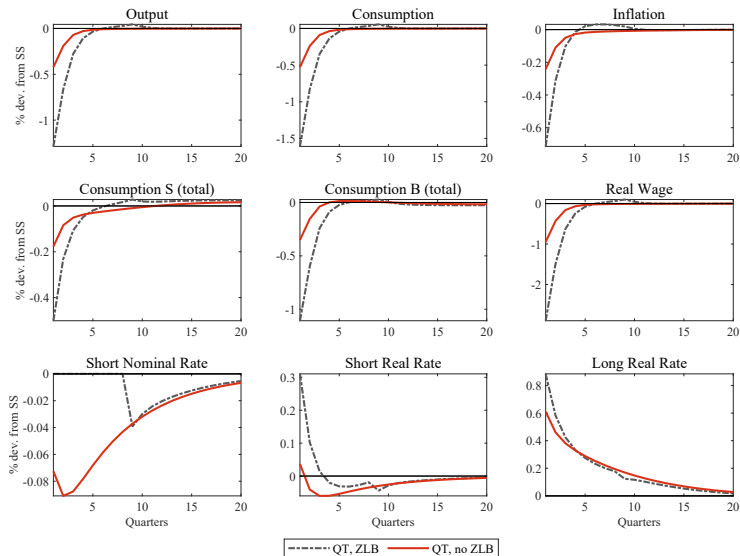
# HHs' budget components: QE/QT shock and QT shock near the ZLB



# HHs' budget components: QE/QT shock and QT shock near the ZLB

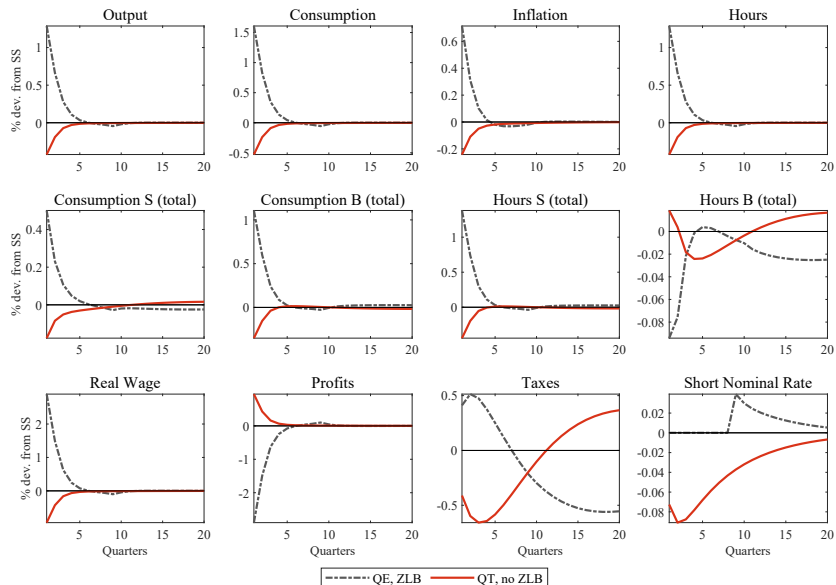


# QT peg vs Taylor rule

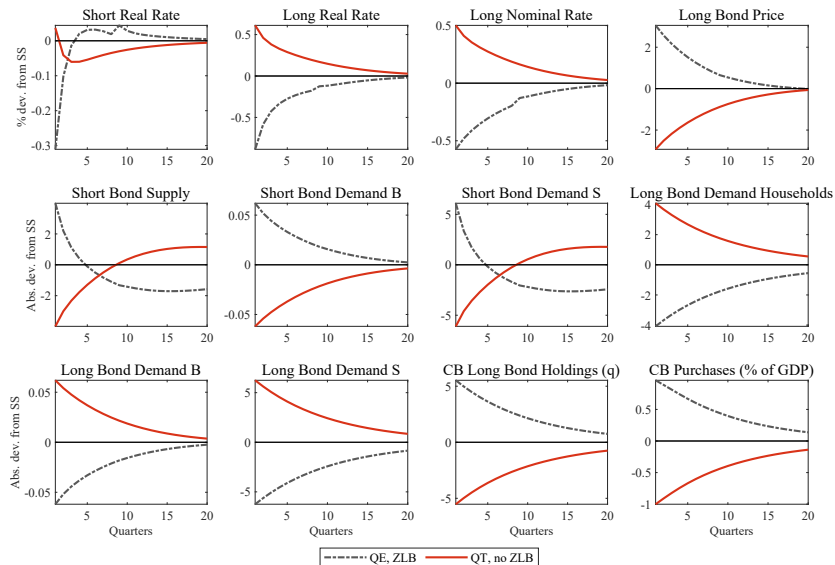




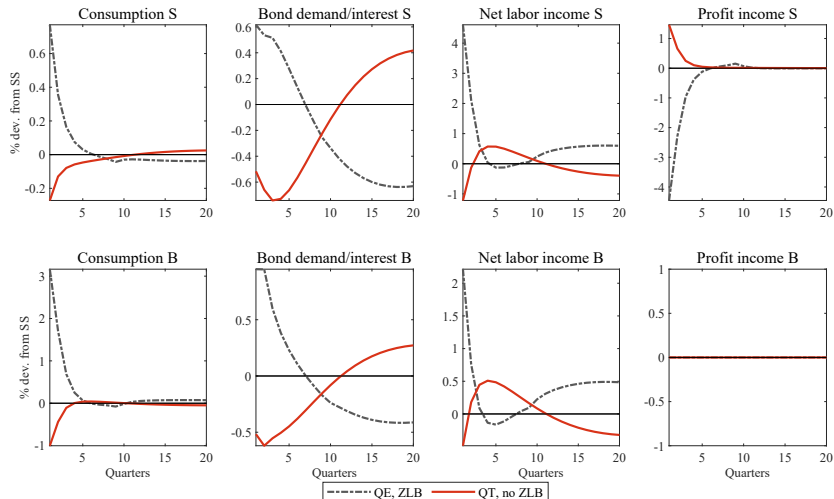
# QE shock ZLB and QT shock off the ZLB (1/2)



# QE shock at ZLB and QT shock off the ZLB (2/2)



# HHs' budget components: QE shock at ZLB and QT shock off the ZLB

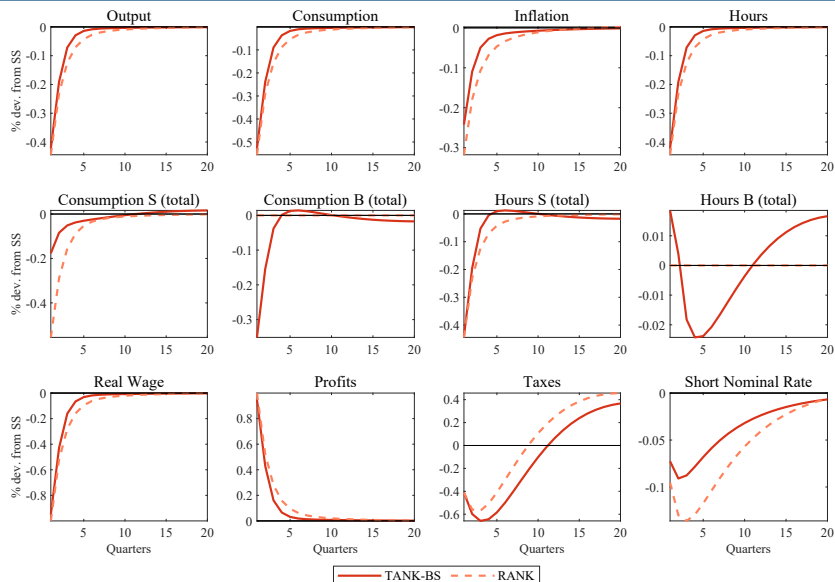


## Multipliers: on impact and cumulated

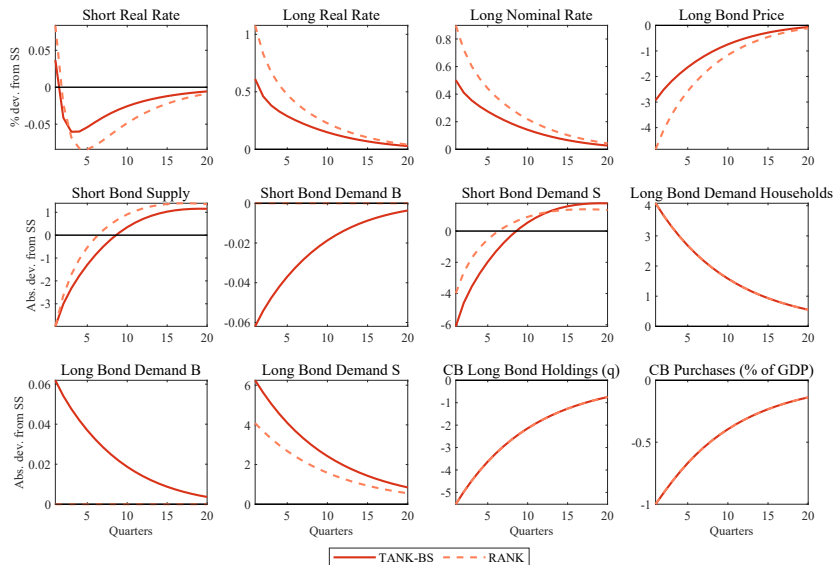
	Output		Inflation		Consumption	
	QE	QT	QE	QT	QE	QT
RANK (impact)	1.05	-0.44	0.70	-0.32	1.32	-0.56
TANK-BS (impact)	1.29	-0.42	0.71	-0.24	1.61	-0.53
RANK (cumulative)	2.18	-0.86	1.32	-0.67	2.72	-1.08
TANK-BS (cumulative)	2.32	-0.71	1.14	-0.43	2.90	-0.89

Multipliers on impact and cumulated over four periods (in %)

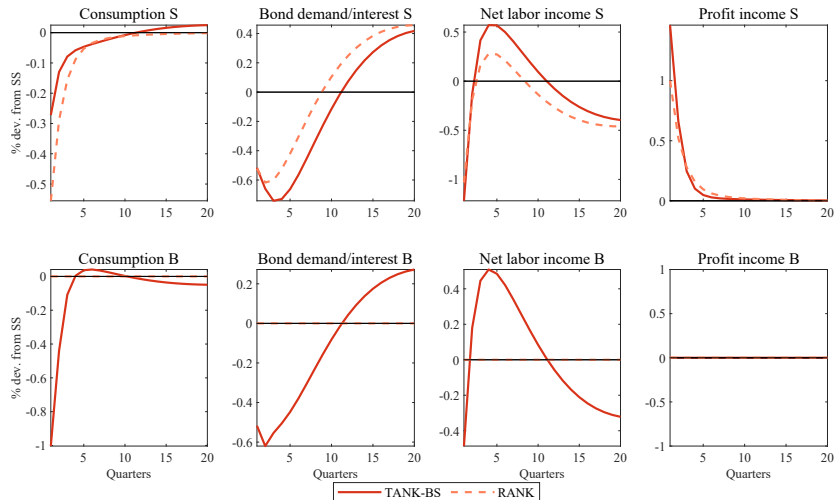
# QT shock off the ZLB: RANK vs. TANK-BS (1/2)



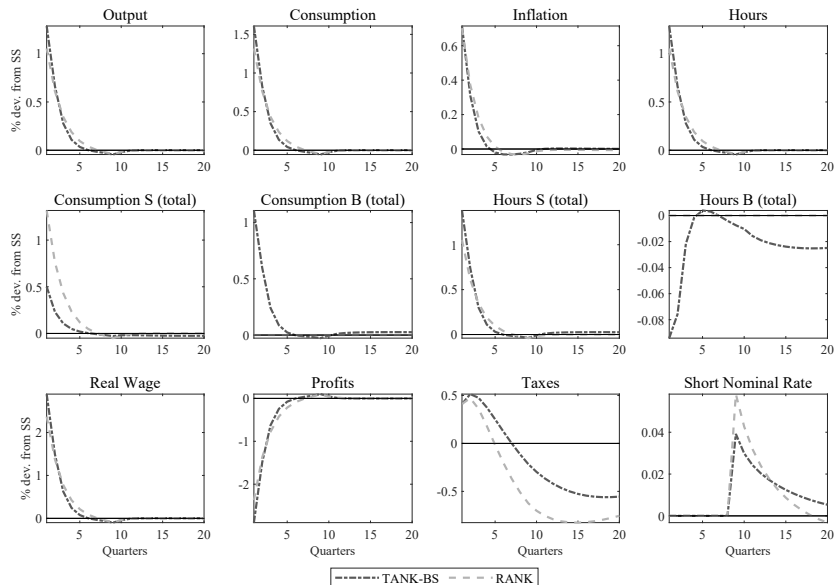
# QT shock off the ZLB: RANK vs. TANK-BS (2/2)



# HHs' budget components: QT shock off the ZLB

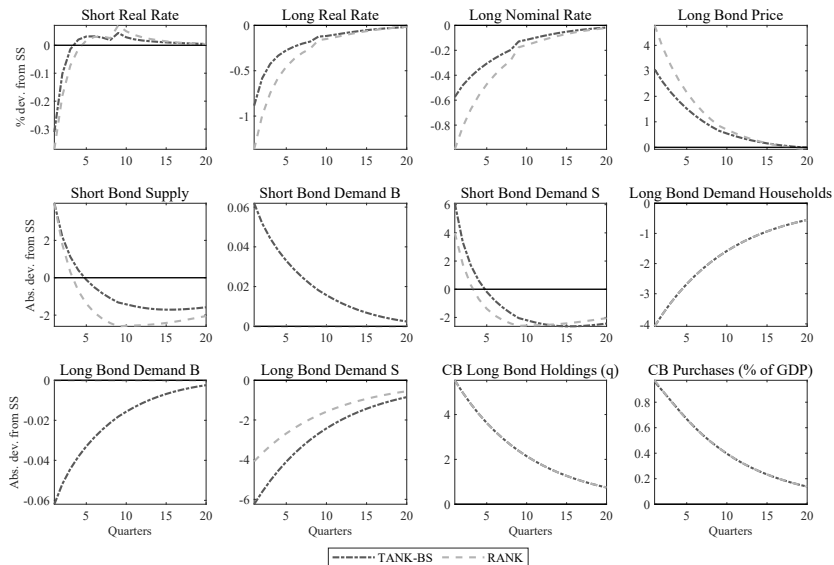


# QE shock at the ZLB: RANK vs. TANK-BS (1/2)

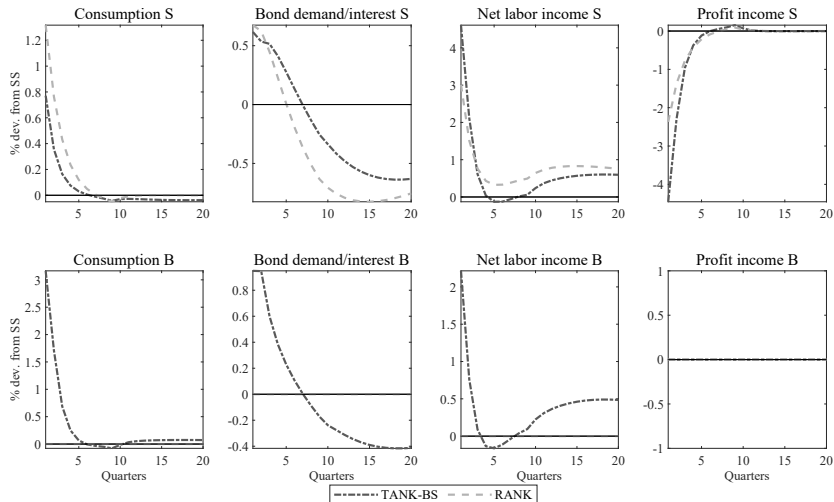




# QE shock at the ZLB: RANK vs. TANK-BS (2/2)



# HHs' budget components: QE shock at the ZLB: RANK vs. TANK-BS



## Robustness: Multipliers on impact of a QE or QT shock

	Output		Inflation		Consumption	
	QE	QT	QE	QT	QE	QT
<i>TANK-BS</i>						
Baseline ( $\tau^D=0, \nu=0.05$ )	1.29	-0.42	0.71	-0.24	1.61	-0.53
$\tau^D = 0.2$	0.81	-0.31	0.52	-0.20	1.02	-0.38
$\tau^D = 0.35$	0.63	-0.26	0.43	-0.18	0.79	-0.32
$\nu = 0.04$	1.05	-0.34	0.58	-0.19	1.31	-0.43
$\nu = 0.06$	1.51	-0.50	0.84	-0.29	1.89	-0.63
<i>RANK</i>						
Baseline ( $\tau^D=0, \nu=0.05$ )	1.05	-0.44	0.70	-0.32	1.32	-0.56
$\tau^D = 0.2$	0.88	-0.39	0.62	-0.29	1.10	-0.49
$\tau^D = 0.35$	0.78	-0.36	0.57	-0.28	0.98	-0.45
$\nu = 0.04$	0.90	-0.36	0.60	-0.26	1.12	-0.45
$\nu = 0.06$	1.20	-0.53	0.79	-0.37	1.50	-0.66